

Toward Security-Oriented Program Analysis

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Joint work with the BINSEC group @ CEA
and many other collaborators

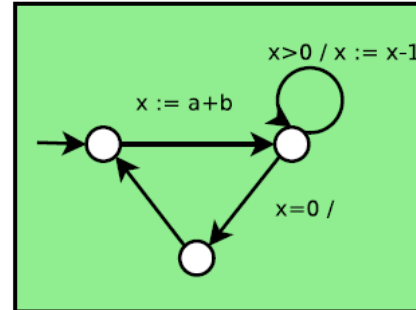


Most attacks come from implementation bugs



A (binary-level) program analysis issue!

Model



Source code

```
int foo(int x, int y) {  
  int k= x;  
  int c=y;  
  while (c>0) do {  
    k++;  
    c--;}  
  return k;  
}
```

Assembly

```
_start:  
  load A 100  
  add B A  
  cmp B 0  
  jle label  
  
label:  
  move @100 B
```

Executable

```
ABFFF780BD70696CA101001BDE45  
145634789234ABFFE678ABDCF456  
5A2B4C6D009F5F5D1E0835715697  
145FEDBCADACBDAD459700346901  
3456KAHA305G67H345BFFADECAD3  
00113456735FFD451E13AB080DAD  
344252FFAADBDA457345FD780001  
FFF22546ADDAE989776600000000
```

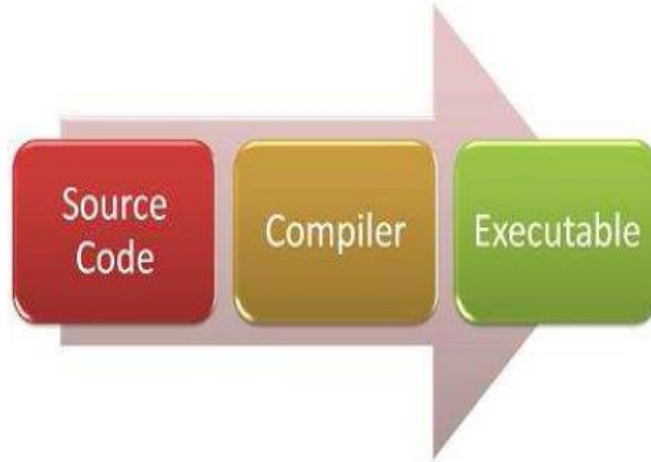
WHY ON BINARY CODE?

No source code



COTS

Post-compilation



Malware comprehension



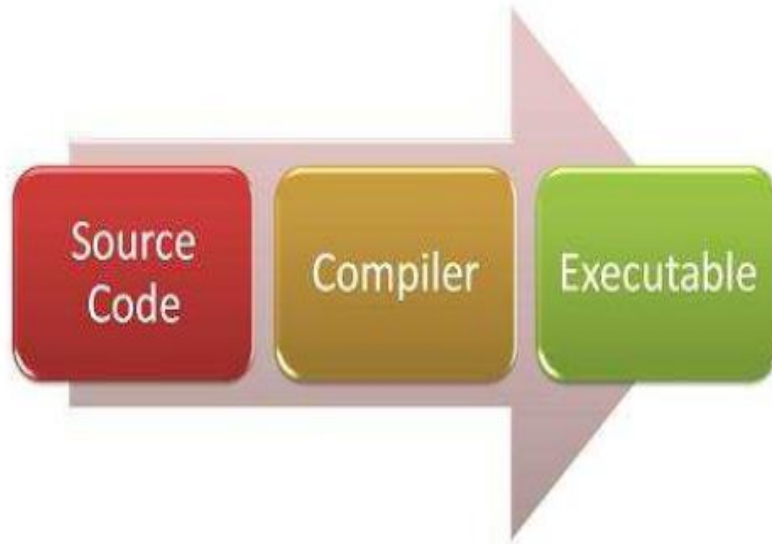
Protection evaluation



Very-low level reasoning



EXAMPLE: COMPILER BUG (?)



- Optimizing compilers may remove dead code
- `pwd` never accessed after `memset`
- Thus can be safely removed
- And allows the password to stay longer in memory

Security bug introduced by a non-buggy compiler

```
void getPassword(void) {
    char pwd [64];
    if (GetPassword(pwd,sizeof(pwd))) {
        /* checkpassword */
    }
    memset(pwd,0,sizeof(pwd));
}
```

OpenSSH CVE-2016-0777

- **secure source code**
- **insecure executable**

BINARY-LEVEL CODE ANALYSIS HAS MANY ADVANTAGES, BUT ...

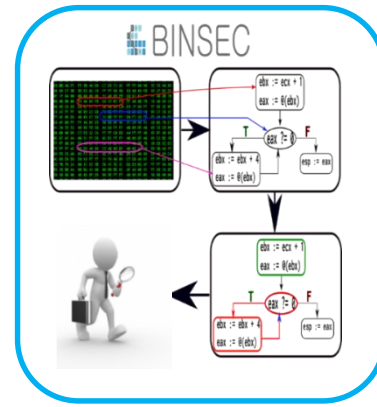


- Focus on code-level security
- Implementation flaws / attacks

- *This talk: our experience on adapting source-level safety analysis to the case of binary-level security [S&P 17, CAV 18, S&P 20, NDSS 21, CAV 21, etc.]*
- **Challenge:** *how to move from safety-oriented code analysis to security-oriented code analysis*
- **Question:** *how does code-level security differ from code-level safety?*

BINSEC: brings formal methods to binary-level security analysis

Break Prove Protect



- Explore many input at once
 - Find bugs
 - Prove security
- Multi-architecture support
 - x86, ARM, RISC-V

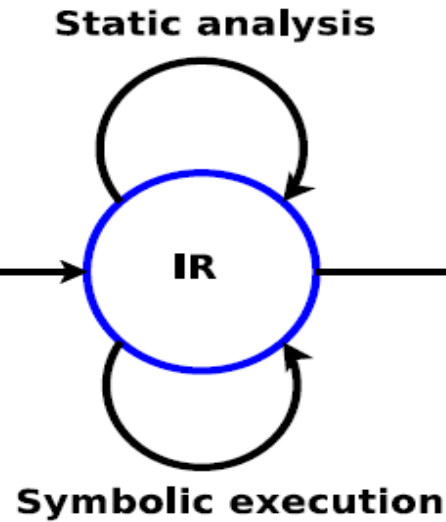
```

x86
ABFFF780BD70696CA101001BDE45
145634789234ABFFE678ABDCF456
5A2B4C6D009F5F5D1E0835715697
145FEDBCADACBDAD459700346901
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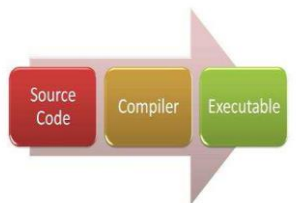
ARM
ABFFF780BD70696CA101001BDE45
145634789234ABFFE678ABDCF456
5A2B4C6D009F5F5D1E0835715697
145FEDBCADACBDAD459700346901
3456KAHA305G67H345BFFADECAD3
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...

ABFFF780BD70696CA101001BDE45
145634789234ABFFE678ABDCF456
5A2B4C6D009F5F5D1E0835715697
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344252FFAADBDA457345FD780001
FFF22546ADDAE989776600000000
    
```



- Advanced reverse
- Vulnerability analysis
- Binary-level security proofs
- Low-level mixt code (C + asm)
- ...



A TOOL OF CHOICE: SYMBOLIC EXECUTION (Godefroid 2005)

[variants, optimizations]



Find real bugs

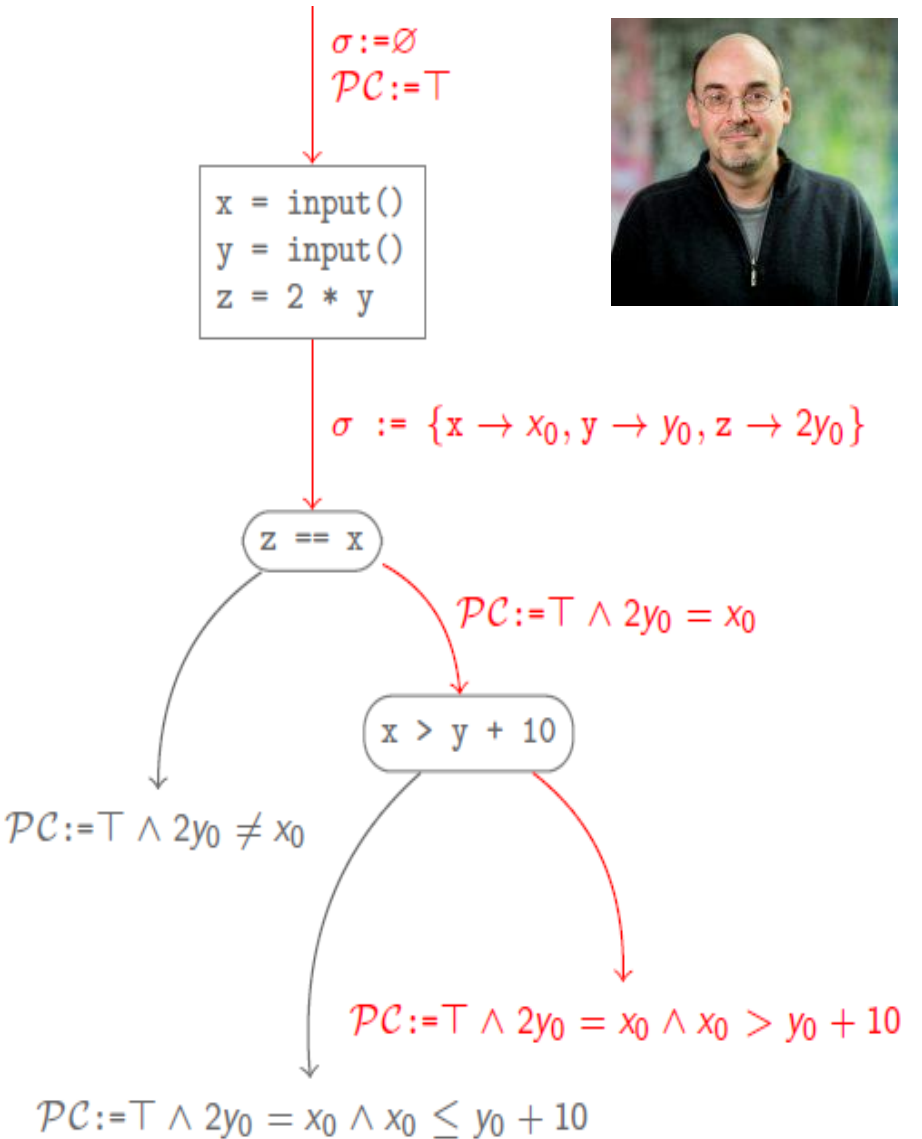
Bounded verification

Robust

```
int main () {
  int x = input();
  int y = input();
  int z = 2 * y;
  if (z == x) {
    if (x > y + 10)
      failure;
  }
  success;
}
```

Given a path of a program

- Compute its « path predicate » f
- Solution of $f \Leftrightarrow$ input following the path
- Solve it with powerful existing solvers



- **Prologue: a little bit of formal methods for safety**
- **Binary-level security analysis: benefits & challenges**
- **The BINSEC platform**
- **From source-level safety to binary-level security: some examples**
- **Conclusion**

ABOUT FORMAL METHODS AND CODE ANALYSIS

- Between Software Engineering and Theoretical Computer Science
- Goal = proves correctness in a mathematical way

- Reason about the meaning of programs

Key concepts : $M \models \varphi$

- M : semantic of the program
- φ : property to be checked
- \models : algorithmic check

- Typical ingredients: transition systems, automata, logic, ...

- Reason about infinite sets of behaviours

Success in (regulated) safety-critical domains

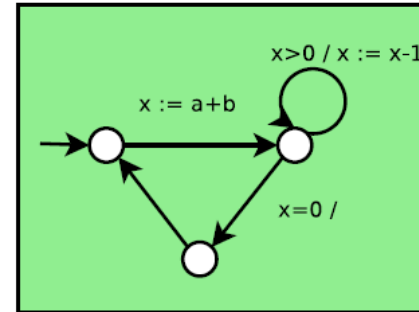


- Prologue: a little bit of formal methods for safety
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NOW: MOVING TO BINARY-LEVEL SECURITY ANALYSIS



Model



Source code

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int foo(int x, int y) {  
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  int c=y;  
  while (c>0) do {  
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    c--;}  
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```

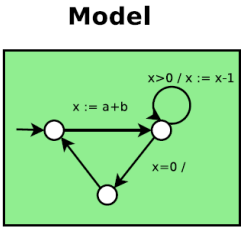
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```



• Binary code

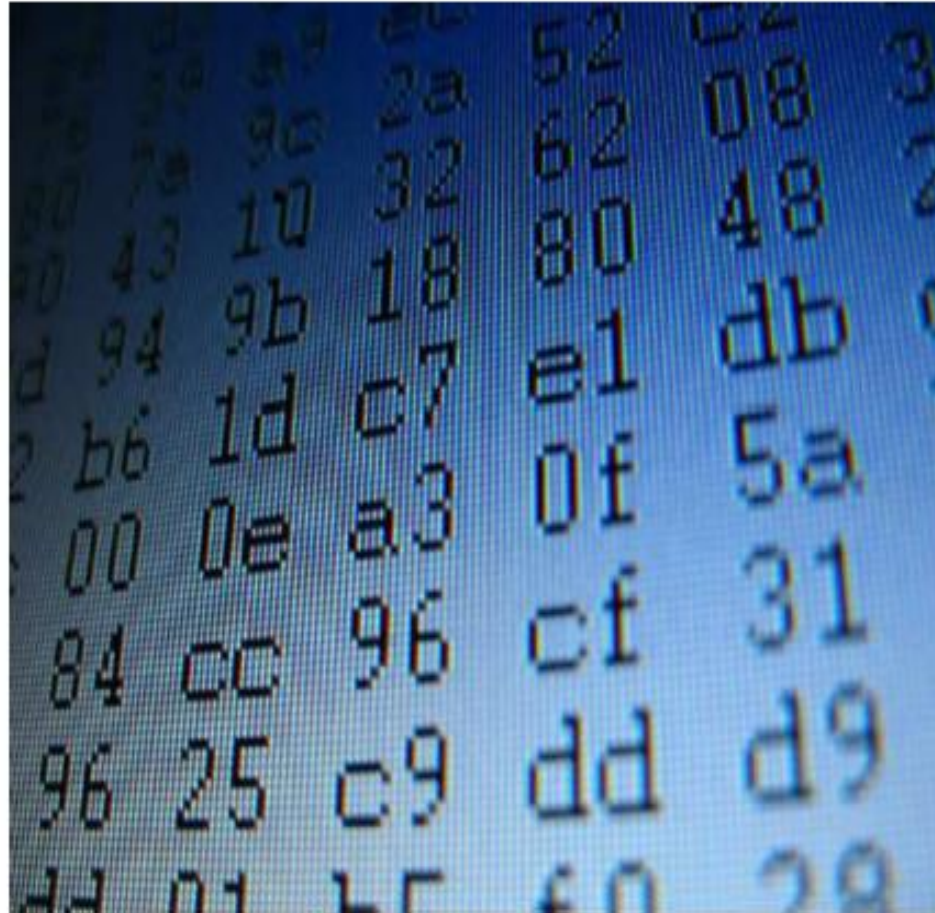
• Attacker

• Properties

- Prologue: a little bit of formal methods for safety
- **Binary-level security analysis: benefits & challenges**
 - Going down to binary
 - Adversarial setting
 - « True security » properties
- The BINSEC platform
- From source-level safety to binary-level security: some examples
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CHALLENGE: BINARY CODE LACKS STRUCTURE

- Instructions?
- Control flow?
- Memory structure?



DISASSEMBLY IS ALREADY TRICKY!

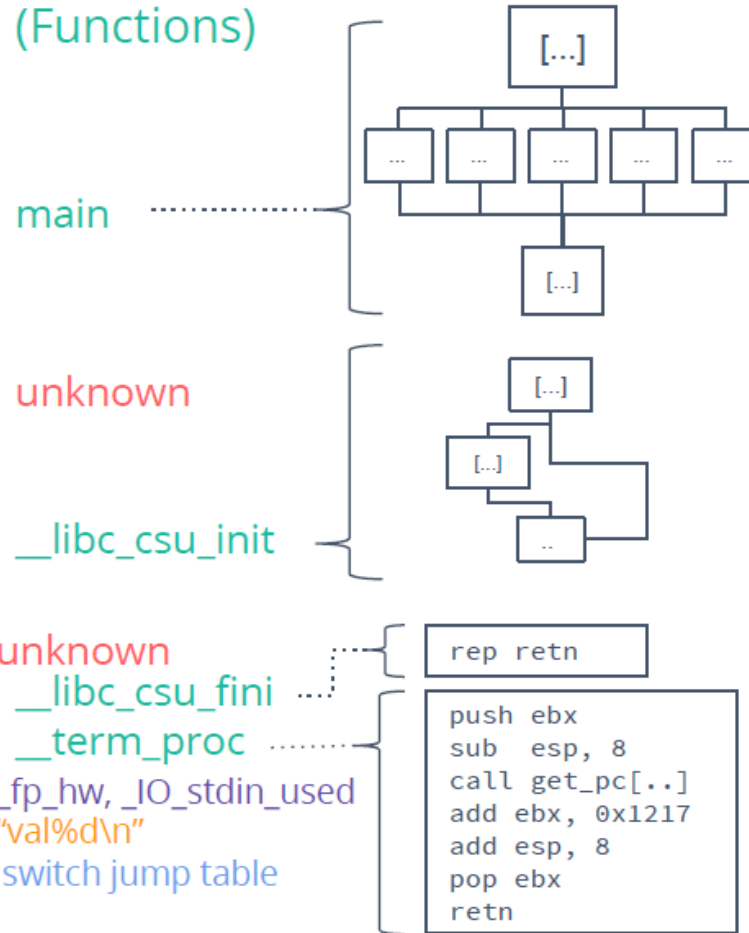
- code – data ??
- dynamic jumps (jmp eax)

Sections

.text	8D 4C 24 04 83 E4 F0 FF 71 FC 55 89 E5 53 51 83
	EC 10 89 CB 83 EC 0C 6A 0A E8 A7 FE FF FF 83 C4
	10 89 45 F0 8B 43 04 83 C0 04 8B 00 83 EC 0C 50
	E8 C0 FE FF FF 83 C4 10 89 45 F4 83 7D F4 04 77
	3B 8B 45 F4 C1 E0 02 05 98 85 04 08 8B 00 FF E0
	C7 45 F4 00 00 00 00 EB 23 C7 45 F4 01 00 00 00
	EB 1A C7 45 F4 02 00 00 00 EB 11 C7 45 F4 03 00
	00 00 EB 08 C7 45 F4 04 00 00 00 90 83 EC 08 FF
	75 F4 68 90 85 04 08 E8 29 FE FF FF 83 C4 10 8B
	45 F4 8D 65 F8 59 5B 5D 8D 61 FC C3 66 90 66 90
	66 90 66 90 90 55 57 31 FF 56 53 E8 85 FE FF FF
	81 C3 89 12 00 00 83 EC 1C 8B 6C 24 30 8D B3 0C
	FF FF FF E8 B1 FD FF FF 8D 83 08 FF FF FF 29 C6
	C1 FE 02 85 F6 74 27 8D B6 00 00 00 00 8B 44 24
	38 89 2C 24 89 44 24 08 8B 44 24 34 89 44 24 04
	FF 94 BB 08 FF FF FF 83 C7 01 39 F7 75 DF 83 C4
	1C 5B 5E 5F 5D C3 EB 0D 90 90 90 90 90 90 90
	90 90 90 90 90 F3 C3 FF FF 53 83 EC 08 E8 13 FE
.fini	FF FF 81 C3 17 12 00 00 83 C4 08 5B C3 03 00 00
.rodata	00 01 00 02 00 76 61 6C 3A 25 64 0A 00 AB 84 04
	08 B4 84 04 08 BD 84 04 08 C6 84 04 08 CF 84 04
	08 01 1B 03 3B 28 00 00 00 04 00 00 00 54 FD FF
.eh_frame_hdr	

■ code ■ dead bytes ■ global csts ■ strings ■ pointers ■ other

Code (Functions)



DISASSEMBLY IS ALREADY TRICKY!

- code – data ??
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Sections

.text	8D 4C 24 04 83 E4 F0 FF 71 FC 55 89 E5 53 51 83
	EC 10 89 CB 83 EC 0C 6A 0A E8 A7 FE FF FF 83 C4
	10 89 45 F0 8B 43 04 83 C0 04 8B 00 83 EC 0C 50
	E8 C0 FE FF FF 83 C4 10 89 45 F4 83 7D F4 04 77
	3B 8B 45 F4 C1 E0 02 05 98 85 04 08 8B 00 FF E0
	C7 45 F4 00 00 00 00 EB 23 C7 45 F4 01 00 00 00
	EB 1A C7 45 F4 02 00 00 00 EB 11 C7 45 F4 03 00
	00 00 EB 08 C7 45 F4 04 00 00 00 90 83 EC 08 FF
	75 F4 68 90 85 04 08 E8 29 FE FF FF 83 C4 10 8B
	45 F4 8D 65 F8 59 5B 5D 8D 61 FC C3 66 90 66 90
	66 90 66 90 90 55 57 31 FF 56 53 E8 85 FE FF FF
	81 C3 89 12 00 00 83 EC 1C 8B 6C 24 30 8D B3 0C
	FF FF FF E8 B1 FD FF FF 8D 83 08 FF FF FF 29 C6
	C1 FE 02 85 F6 74 27 8D B6 00 00 00 00 8B 44 24
	38 89 2C 24 89 44 24 08 8B 44 24 34 89 44 24 04
	FF 94 BB 08 FF FF FF 83 C7 01 39 F7 75 DF 83 C4
	1C 5B 5E 5F 5D C3 EB 0D 90 90 90 90 90 90 90
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	08 01 1B 03 3B 28 00 00 00 04 00 00 00 54 FD FF
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Code (Functions)

main

unknown

__libc_csu_init

unknown

__libc_csu_fini

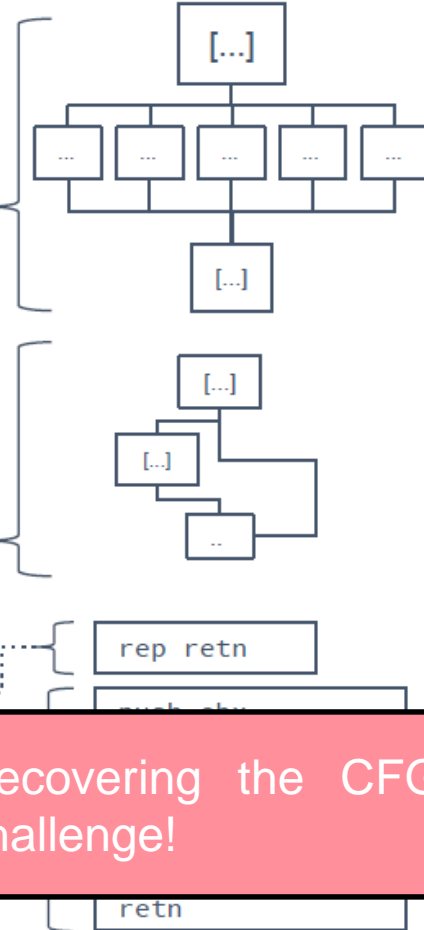
__term_pr

_fp_hw, _IO_s

"val%d\n"

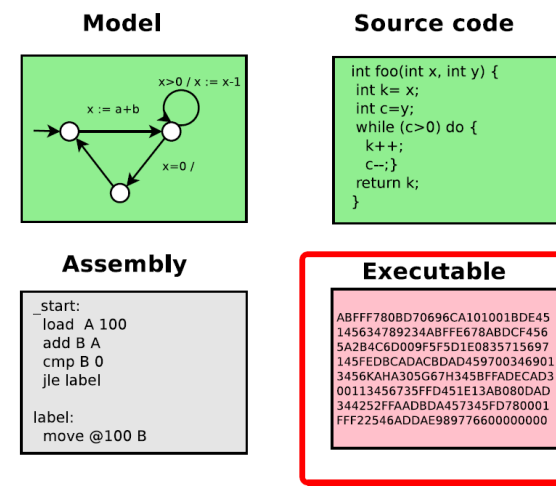
switch jump

Assembly



• Recovering the CFG is already a challenge!

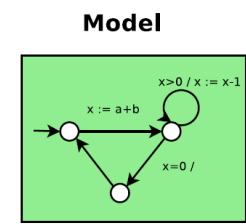
BINARY-LEVEL ANALYSIS



- Low-level control (CFG?)
- Low-level data & memory

Machine codes are complex

BINARY-LEVEL ANALYSIS



Source code

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  while (c>0) do {
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3456KAHA305G67H345BFFADECAD3
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344252FFAADBDA457345FD780001
FFF22546ADDAE989776600000000
```



Break an implicit assumption in code analysis

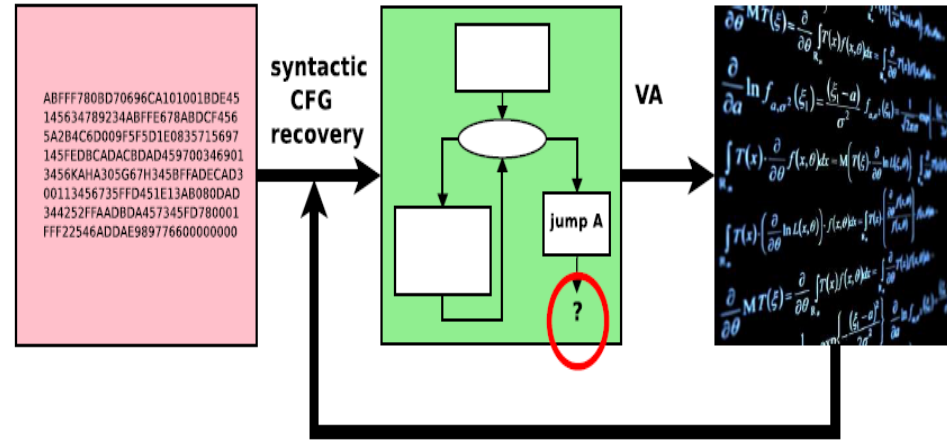
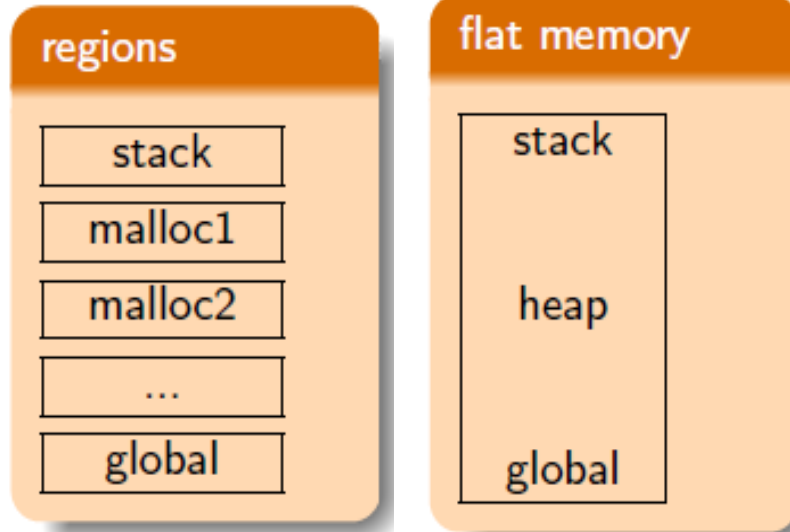
- Low-level control (CFG?)
- Low-level data & memory

At the edge of current methods

- Solved problem
- IR

Machine codes are complex

BINARY CODE SEMANTIC LACKS STRUCTURE



Problems


- Jump eax
- Untyped memory
- Bit-level reasoning

```
if (ax > bx) X = -1;
else X = 1;
```

```
OF := ((ax{31,31}#bx{31,31}) &
      (ax{31,31}#(ax-bx){31,31}));
SF := (ax-bx) < 0;
ZF := (ax-bx) = 0;
if (¬ ZF ^ (OF = SF)) goto l1
X := 1
goto l2
l1: X := -1
l2:
```

BINARY CODE SEMANTIC LACKS STRUCTURE

```
if (ax > bx) X = -1;  
else X = 1;
```



```
OF := ((ax{31,31}≠bx{31,31}) &  
        (ax{31,31}≠(ax-bx){31,31}));  
SF := (ax-bx) < 0;  
ZF := (ax-bx) = 0;  
if (¬ ZF ∧ (OF = SF)) goto l1  
X := 1  
goto l2  
l1: X := -1  
l2:
```

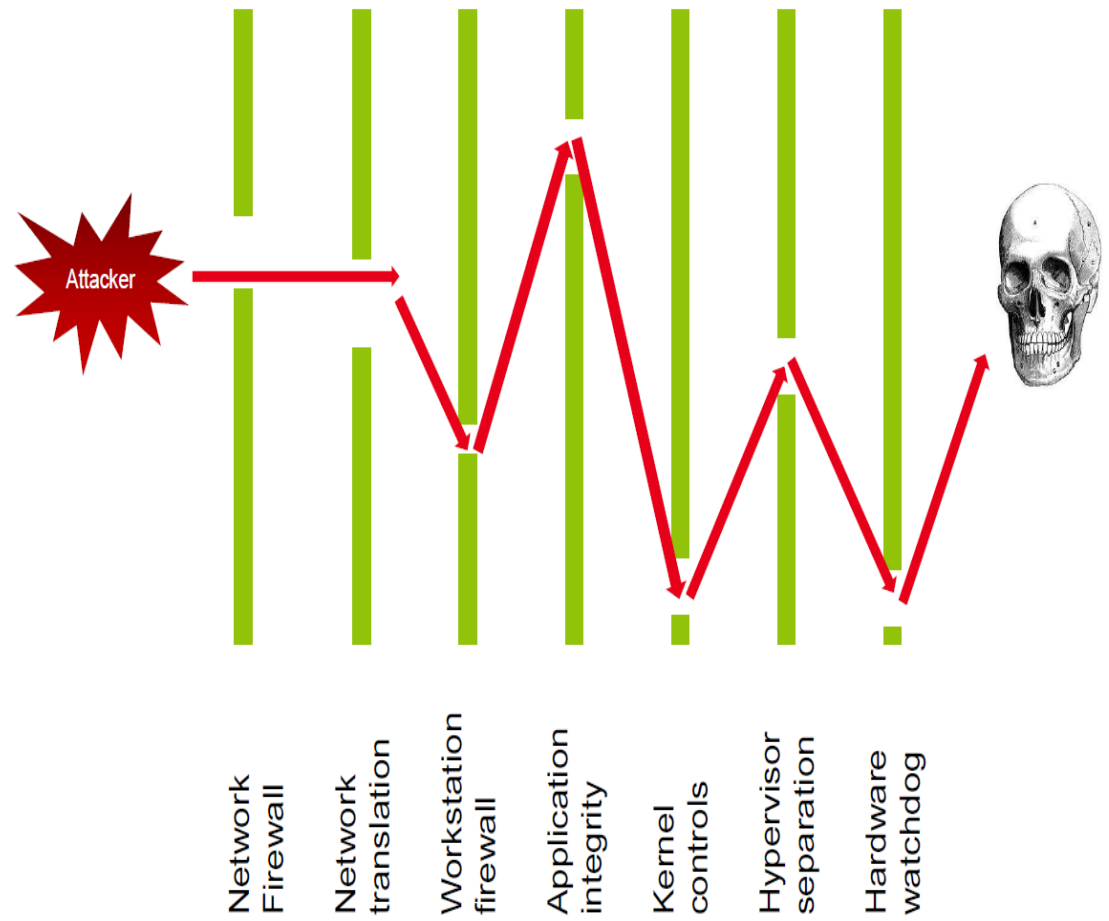
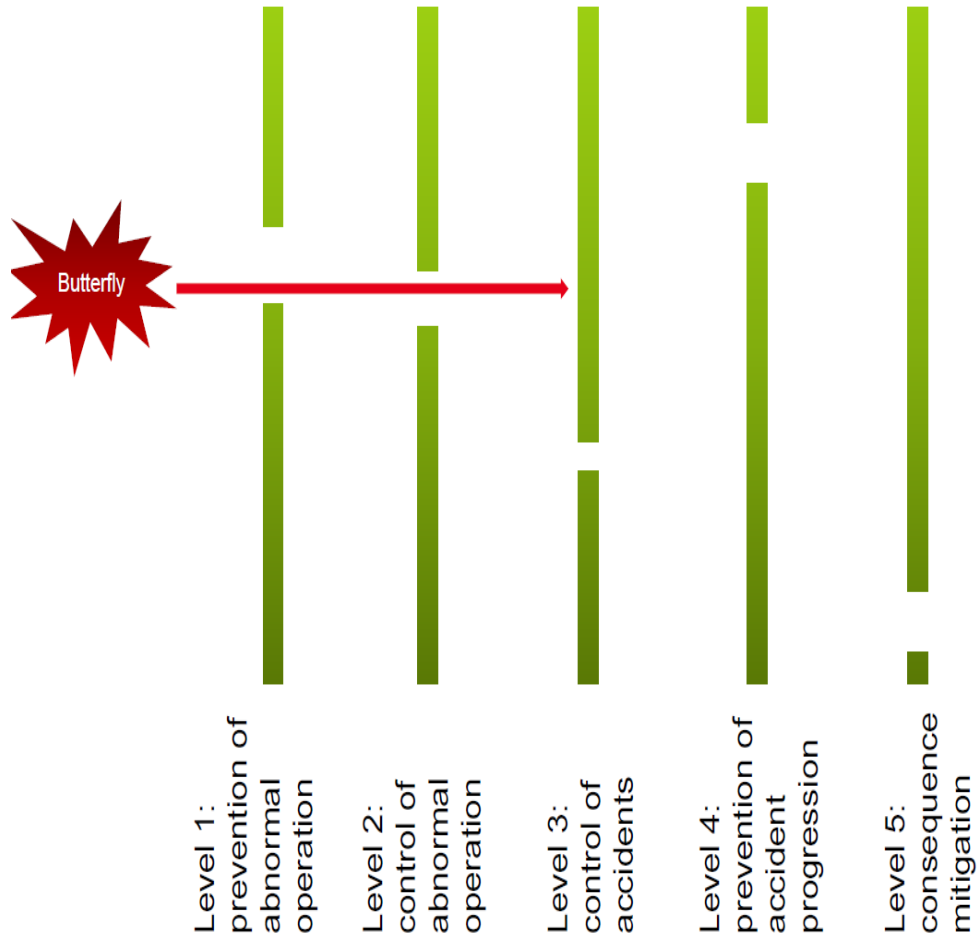
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 - **Adversarial setting**
 - « True security » properties
- **The BINSEC platform**
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CHALLENGE: ATTACKER



Nature is not nice

Attacker is evil



ATTACKER in Standard Program Analysis

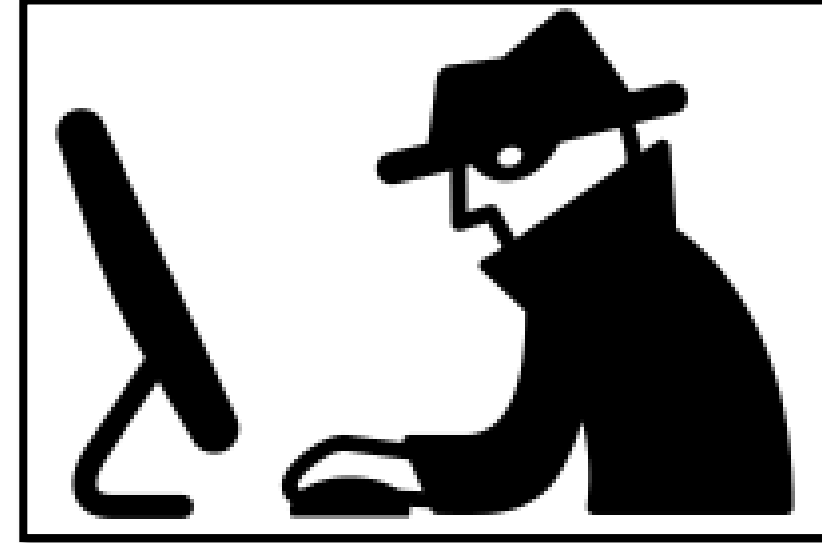


- We are reasoning worst case: seems very powerful!

ATTACKER in Standard Program Analysis

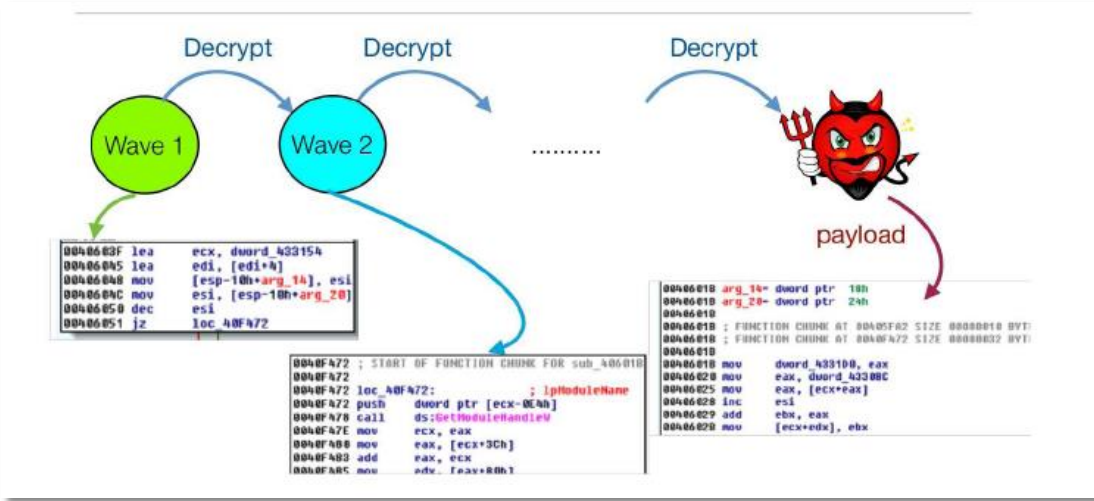


- **We are reasoning worst case: seems very powerful!**
- **Still, our current attacker plays the rules: respects the program interface**
 - Can craft very smart input, but only through expected input sources



- **We are reasoning worst case: seems very powerful!**
- **Still, our attacker plays the rules: respects the program interface**
 - Can craft very smart input, but only through expected input sources
- **What about someone who do not play the rules?**
 - Side channel attacks
 - Micro-architectural attacks

ADVERSARIAL BINARY CODE



address	instr
80483d1	call +5
80483d6	pop edx
80483d7	add edx, 8
80483da	push edx
80483db	ret
80483dc	.byte{invalid}
80483de	[...]

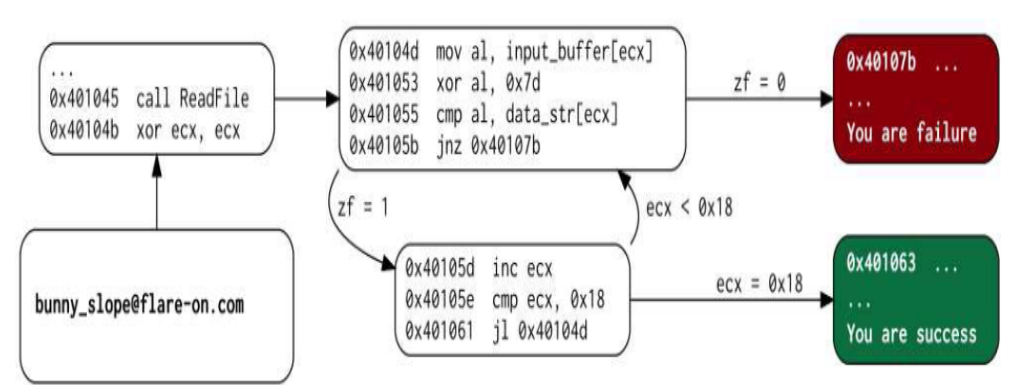


- self-modification
- encryption
- virtualization
- code overlapping
- opaque predicates
- callstack tampering
- ...

eg: $7y^2 - 1 \neq x^2$
 (for any value of x, y in modular arithmetic)

```

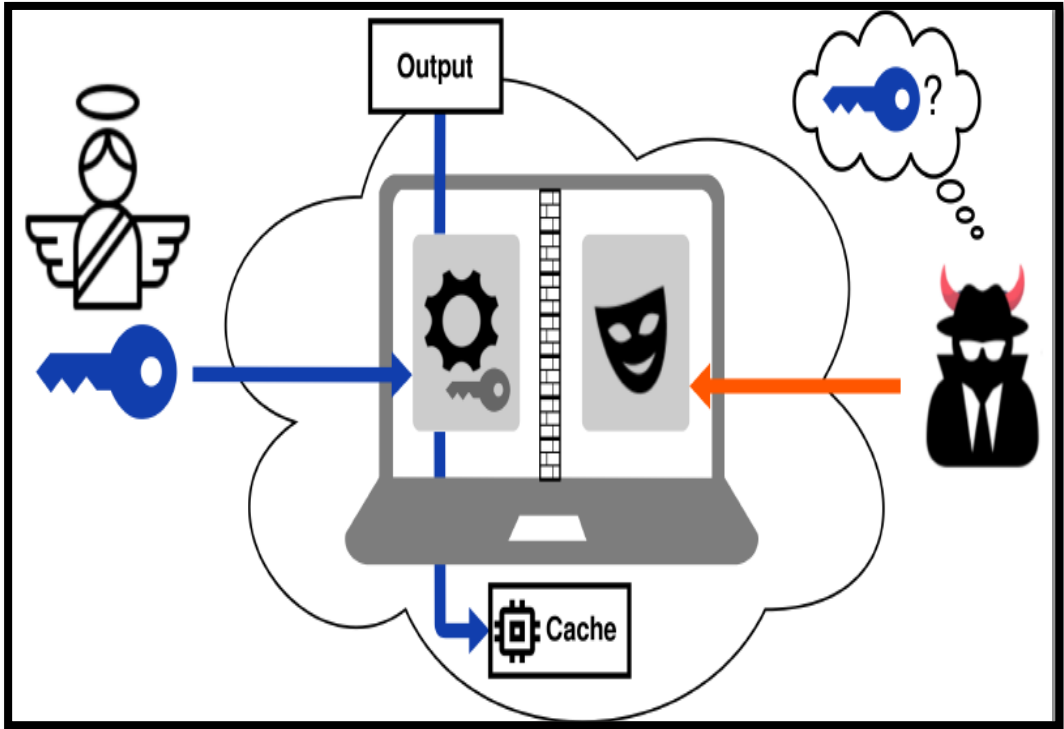
mov  eax, ds:X
mov  ecx, ds:Y
imul ecx, ecx
imul ecx, 7
sub  ecx, 1
imul eax, eax
cmp  ecx, eax
jz   <dead_addr>
    
```



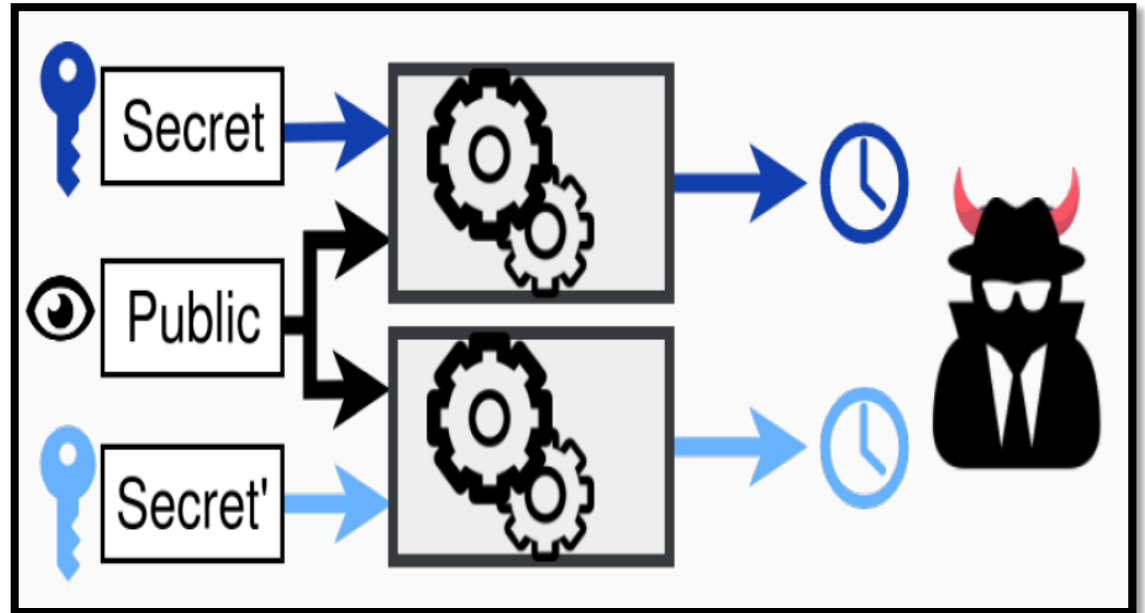
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EXAMPLE: TIMING ATTACKS

Information leakage



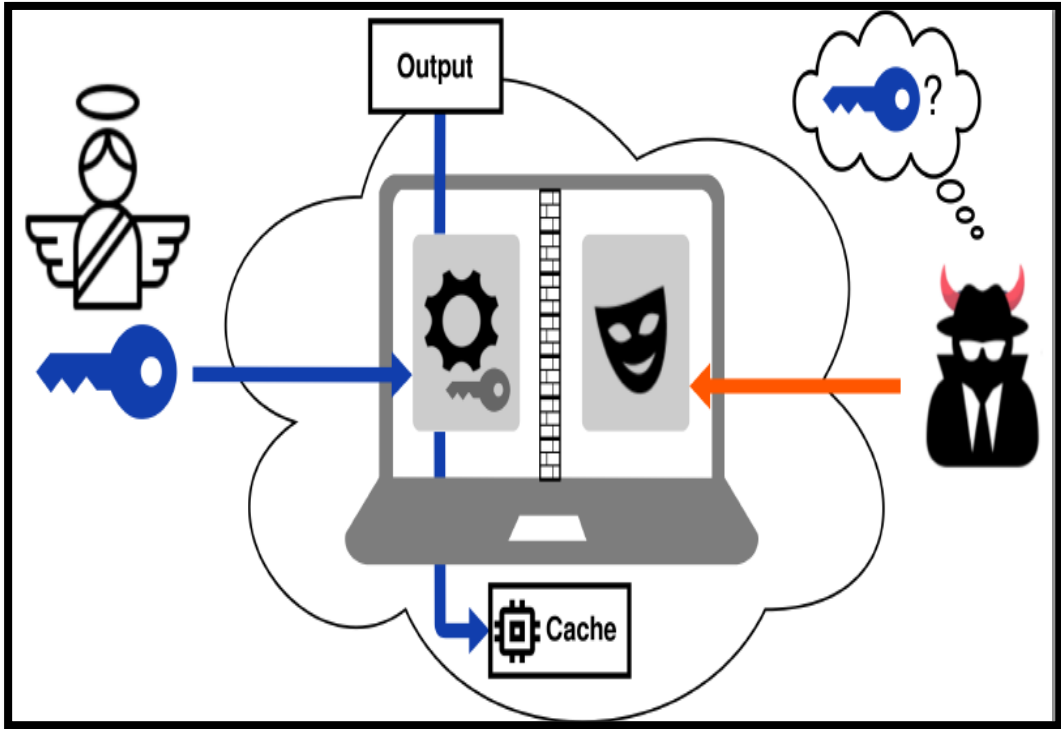
Properties over pairs of executions



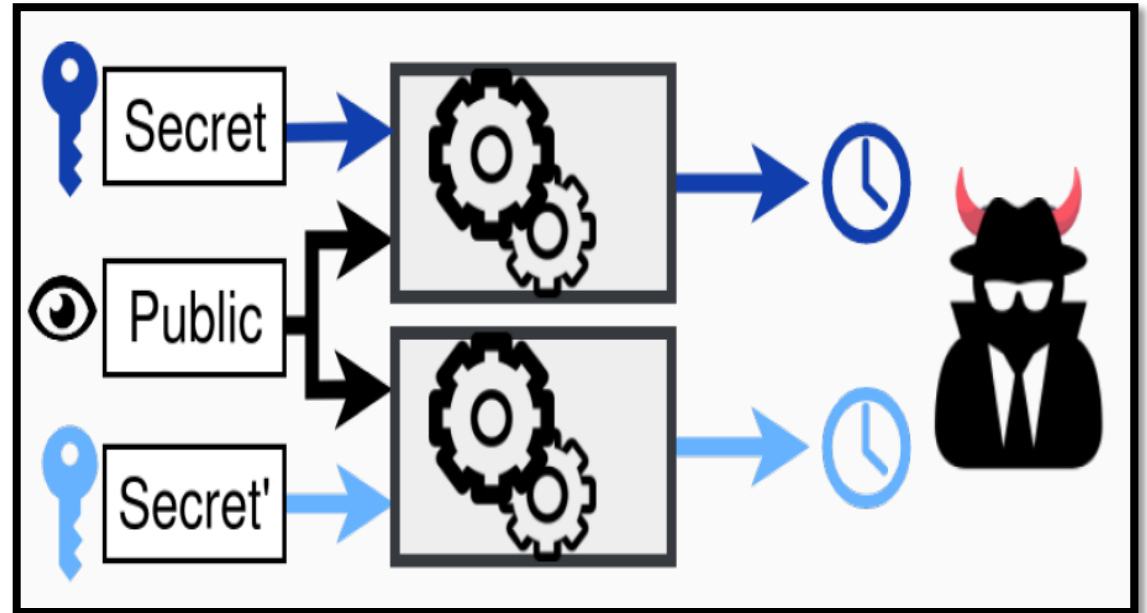
EXAMPLE: TIMING ATTACKS

- Hyperproperties
- Quantitative

Information leakage



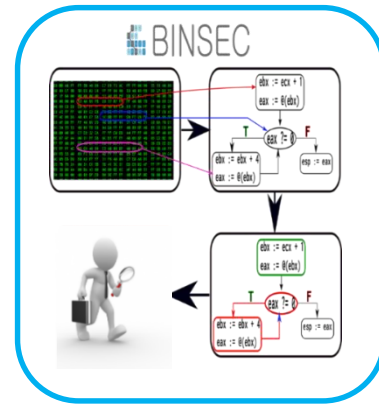
Properties over pairs of executions



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 - x86, ARM, RISC-V

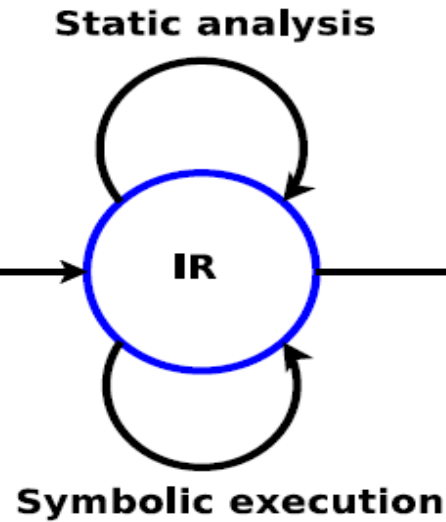
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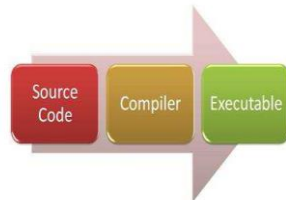
ARM
ABFFF780BD70696CA101001BDE45
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...

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344252FFAADBDA457345FD780001
FFF22546ADDAE989776600000000
    
```



- Advanced reverse
- Vulnerability analysis
- Binary-level security proofs
- Low-level mixt code (C + asm)
- ...



Binsec intermediate representation

```
inst := lv ← e | goto e | if e then goto e
lv   := var | @[e]n
e    := cst | lv | unop e | binop e e | e ? e : e

unop := ¬ | − | uextn | sextn | extracti..j
binop := arith | bitwise | cmp | concat
arith := + | − | × | udiv | urem | sdiv | srem
bitwise := ∧ | ∨ | ⊕ | shl | shr | sar
cmp := = | ≠ | >u | <u | >s | <s
```

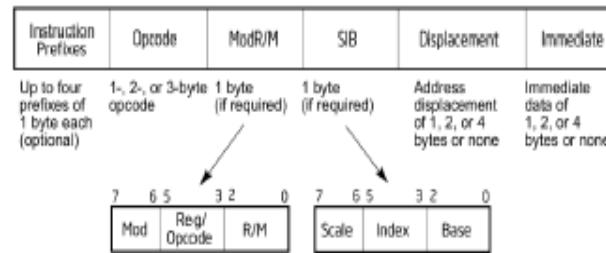
Multi-architecture

x86-32bit – ARMv7

- lhs := rhs
- goto addr, goto expr
- ite(cond)? goto addr

- **Concise**
- **Well-defined**
- **Clear, side-effect free**

INTERMEDIATE REPRESENTATION



- Concise
- Well-defined
- Clear, side-effect free

81 c3 57 1d 00 00 $\xrightarrow{x86reference}$ ADD EBX 1d57

```
(0x29e,0) tmp := EBX + 7511;
(0x29e,1) OF := (EBX{31,31}=7511{31,31}) && (EBX{31,31}<>tmp{31,31});
(0x29e,2) SF := tmp{31,31};
(0x29e,3) ZF := (tmp = 0);
(0x28e,4) AF := ((extu (EBX{0,7}) 9) + (extu 7511{0,7} 9)){8,8};
(0x29e,6) CF := ((extu EBX 33) + (extu 7511 33)){32,32};
(0x29e,7) EBX := tmp; goto (0x2a4,0)
```

Key 2: SYMBOLIC EXECUTION (Godefroid 2005)

[variants, optimizations]

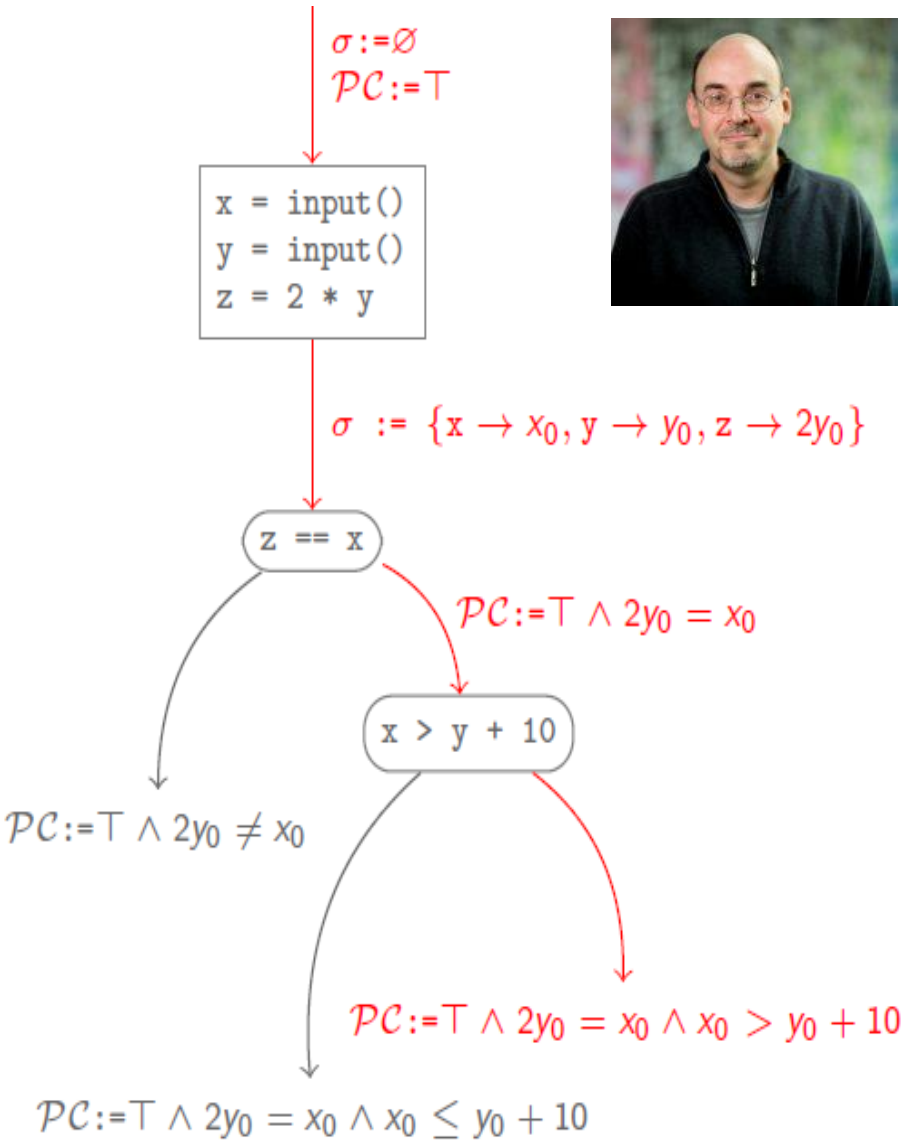


Find real bugs

Bounded verification

Robust

```
int main () {
  int x = input();
  int y = input();
  int z = 2 * y;
  if (z == x) {
    if (x > y + 10)
      failure;
  }
  success;
}
```

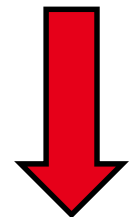
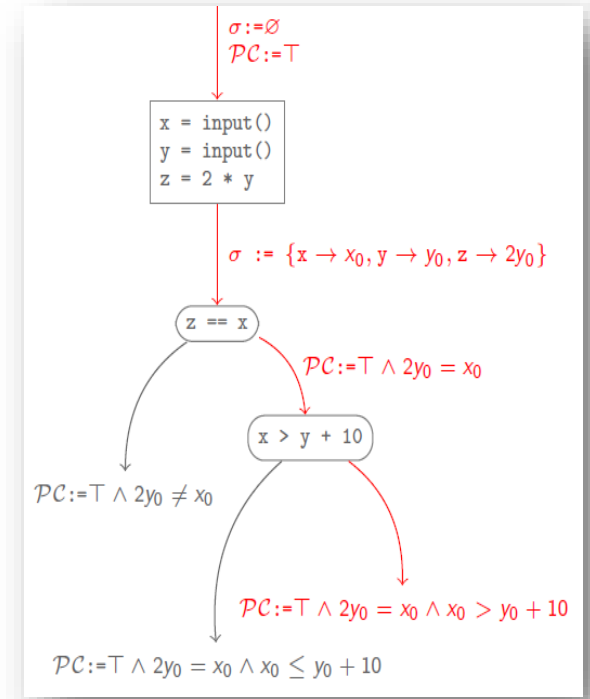


- Given a path of a program
- Compute its « path predicate » f
 - Solution of $f \Leftrightarrow$ input following the path
 - Solve it with powerful existing solvers



PATH PREDICATE COMPUTATION & SOLVING

Loc	Instruction
0	input(y,z)
1	w := y+1
2	x := w + 3
3	if (x < 2 * z) (branche True)
4	if (x < z) (branche False)



let $W_1 \triangleq Y_0 + 1$ in
 let $X_2 \triangleq W_1 + 3$ in
 $X_2 < 2 \times Z_0 \wedge X_2 \geq Z_0$

Blackbox solvers

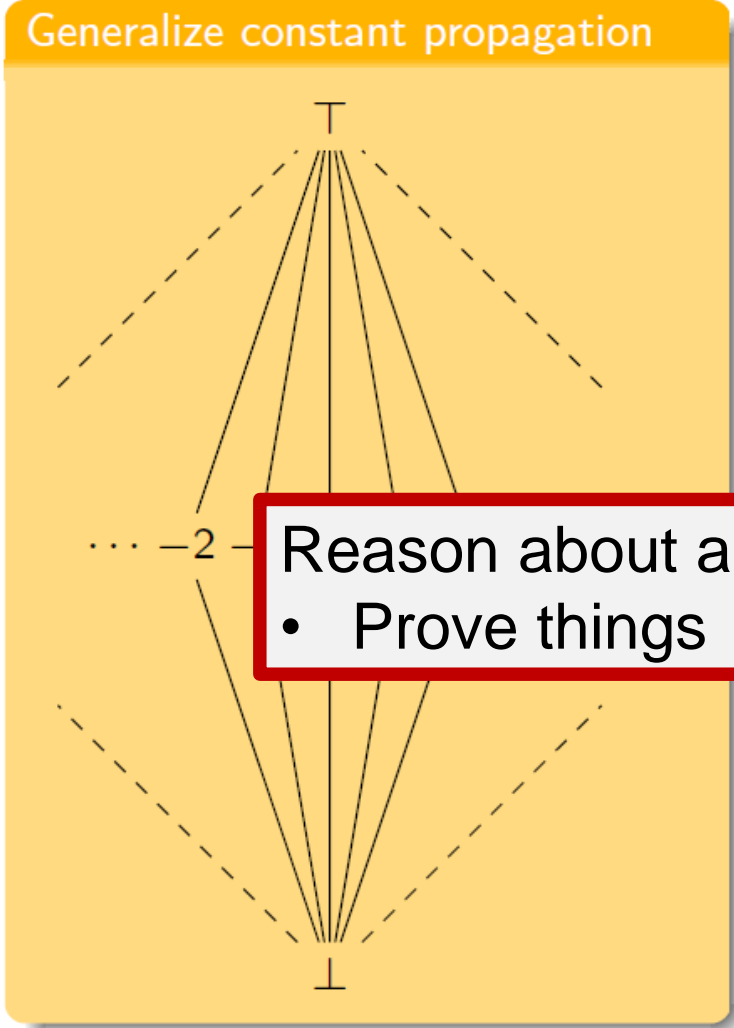
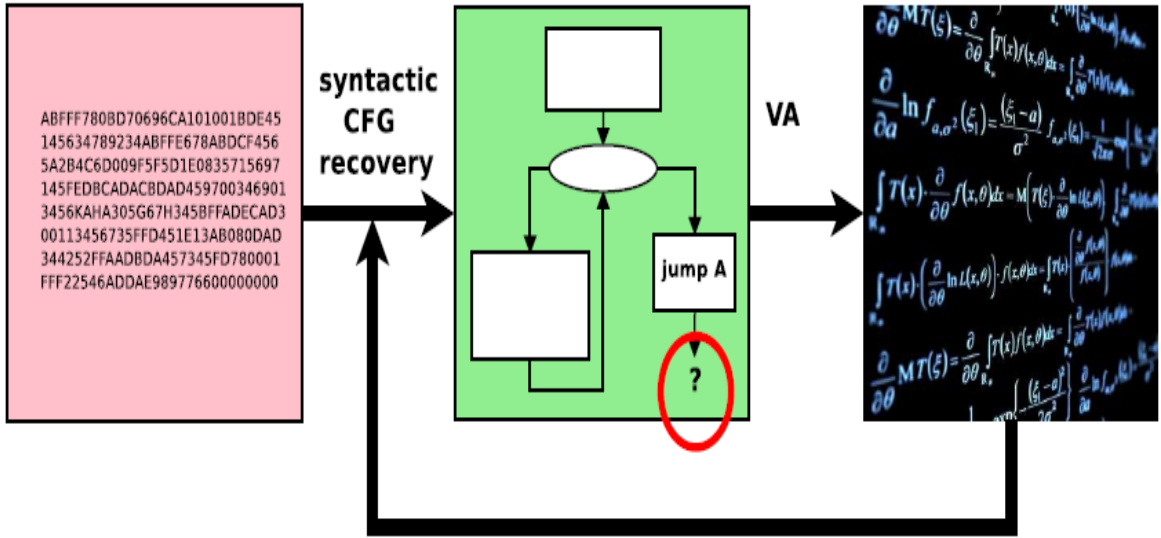


my input!!

$Y_0 = 0 \wedge Z_0 = 3$

ALSO: STATIC SEMANTIC ANALYSIS (harder, doable on *some* classes of programs)

Complete verification

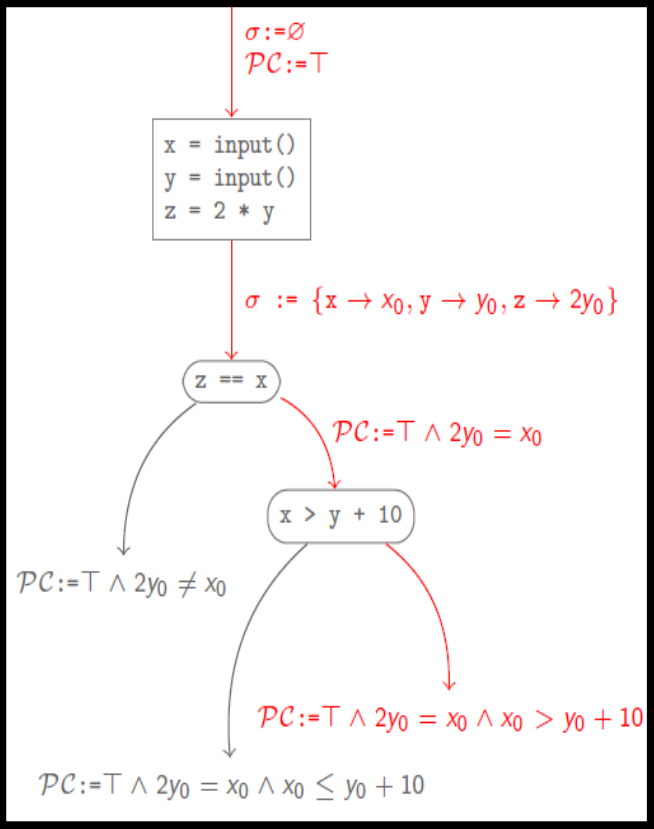


Framework : abstract interpretation

- notion of abstract domain
 $\perp, \top, \sqcup, \sqcap, \sqsubseteq, \text{eval}^\#$
- more or less precise domains
. intervals, polyhedra, etc.
- fixpoint until stabilization

- Prologue: a little bit of formal methods for safety
- Binary-level security analysis: benefits & challenges
- The BINSEC platform
- **From source-level safety to binary-level security: some examples**
- Conclusion

Case 1: Vulnerability finding with symbolic execution (Godefroid et al., Cadar et al., Sen et al.)



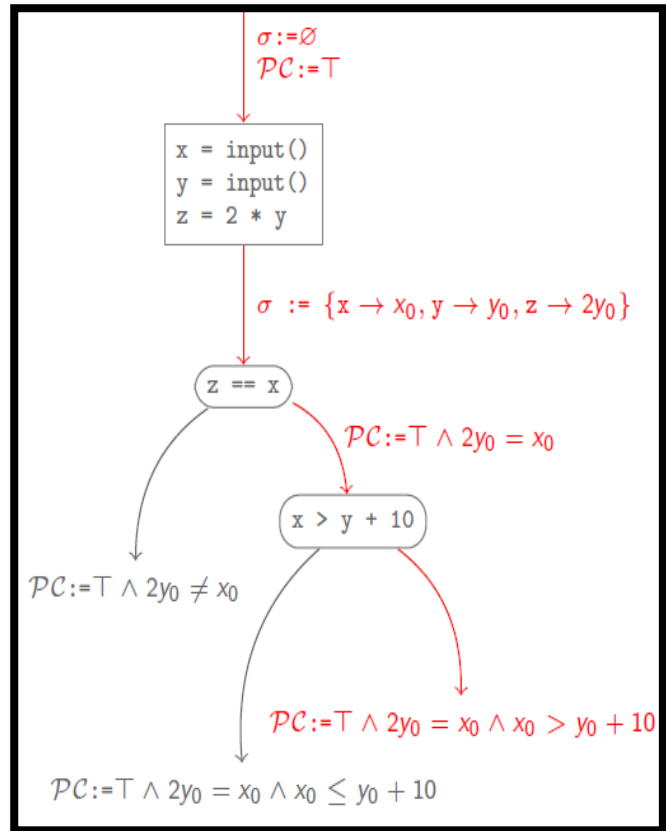
- ▶ Intensive path exploration
- ▶ Target critical bugs

Challenge = path explosion



Find a needle in the heap!

Case 1: Vulnerability finding with symbolic execution (Heelan, Brumley et al.)



- ▶ Intensive path exploration
- ▶ Target critical bugs
- ▶ Directly create simple exploits



Challenge = path explosion



Find a needle in the heap!

Case 1: What about hard-to-find bugs [SSPREW'16](with Josselin Feist et al.)



```

4800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
0000 00b8 4500 0000 5dc3 0820 0000 00b8 4500 000
bf0e 0821 0000 00b8 5800 5589 e5c7 0540 bf0e 0821 0000 00b
e5c7 0540 bf0e 0822 0000 0000 5dc3 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec1
0000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 088
8b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08f
00c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
0000 00e9 d901 0000 c645 0548 bf0e 0882 0000 00e9 d901 000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
48bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
0600 0000 e988 0100 00e9 c705 48bf 0e08 0600 0000 e988 010
f701 c645 f800 c645 f900 0301 0000 c645 f701 c645 f800 c64
fc00 740f c705 48bf 0e08 c645 fa02 807d fc00 740f c705 48b
0100 00e9 5901 0000 c645 0400 0000 e95e 0100 00e9 5901 000
c645 f900 c645 fa03 807d f701 c645 f800 c645 f900 c645 fa0
fe00 7506 c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 7506 c705 48bf 0e08 0500 0000 807d fc00 750a c705 48b
fe00 740f c705 48bf 0e08 0300 0000 807d fc00 740f c705 48b
0100 9901 0000 c645 0600 0000 e90e 0100 00e9 9901 000
c645 0405 fa04 807d f701 c645 f800 c645 f901 c645 fa0
48bf 0e08 0400 0000 e9c4 fd00 750f c705 48bf 0e08 0400 000
0000 c645 f701 c645 f800 0000 00e9 df00 0000 c645 f701 c64
fa04 807d fc00 7410 807d c645 f900 c645 fa04 807d fc00 741
48bf 0e08 0700 0000 807d ff00 750a c705 48bf 0e08 0700 000
ff00 740f c705 48bf 0e08 fc00 7410 807d ff00 740f c705 48b
0000 00e9 9900 0000 c645 0600 0000 e99e 0000 00e9 9900 000
c645 f900 c645 fa05 807d f701 c645 f800 c645 f900 c645 fa0
fc00 750a c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 750a c705 48bf 0e08 0800 0000 807d fc00 750a c705 48b
fe00 7506 807d ff00 740c 0900 0000 807d fe00 7506 807d ff0
0600 0000 eb4b eb49 c645 c705 48bf ce08 0600 0000 eb4b eb4
c645 f901 c645 fa02 807d f701 c645 f800 c645 f901 c645 fa0
5dc3 5589 e5c7 0540 bf0e 00b8 5400 0000 5dc3 5589 e5c7 054
1800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
3000 00b8 4500 0000 5dc3 0540 bf0e 0820 0000 00b8 4500 000
jF0e 0821 0000 00b8 5800 5589 e5c7 0540 bf0e 0821 0000 00b
25c7 0540 bf0e 0822 0000 0000 5dc3 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec10
3000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 0883
3b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08ff
30c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
3000 00e9 d901 0000 c645 0548 bf0e 0882 0000 00e9 d901 000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
18bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 0000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
3600 0000 e988 0100 00e9 c705 48bf 0e08 0600 0000 e988 010

```

Entry point

free

use

Use-after-free bugs

- Very hard to find
- Sequence of events
- DSE gets lost



Find a needle in the heap!

Case 1: What about hard-to-find bugs [SSPREW'16](with Josselin Feist et al.)



Use-after-free bugs

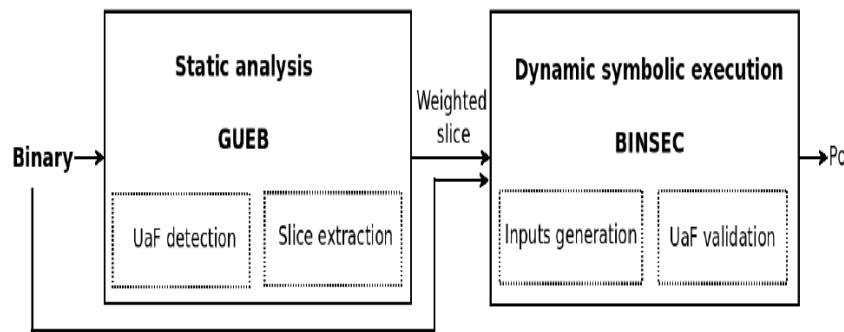
- Very hard to find
- Sequence of events
- DSE lost

```

4800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
0000 00b8 4500 0000 0000 0820 0000 00b8 4500 0000
bf0e 0821 0000 00b8 5589 e5c7 0812 0000 00b8
e5c7 0540 bf0e 0822 0000 00b8 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec1
0000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 088
8b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08f
00c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
0000 00c9 d901 0000 c645 0548 bf0e 0882 0000 00c9 d901 000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
48bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
0600 0000 e988 0100 00e9 c705 48bf 0e08 0600 e988 010
f701 c645 f800 c645 f900 8001 0000 c645 f701 c645 f800 c64
fc00 740f c705 48bf 0e08 c645 fa02 807d fc00 740f c705 48b
0100 00e9 5901 0000 c645 0400 0000 e95e 0100 00e9 5901 000
c645 f900 c645 fa03 807d f701 c645 f800 c645 f900 c645 fa0
fe00 750a c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 750a c705 48bf 0e08 0500 0000 807d fc00 750a c705 48b
fe00 740f c705 48bf 0e08 0300 0000 807d fe00 740f c705 48b
0100 0000 e988 0100 00e9 c705 48bf 0e08 0600 e988 010
c645 f900 c645 fa03 807d f701 c645 f800 c645 f901 c645 fa0
48bf 0e08 0000 c9c4 f400 c645 f800 c645 f901 c645 fa0
0000 c645 f701 c645 f800 0000 c645 f800 c645 f901 c645 fa0
fa04 807d fc00 7410 807d c645 f900 c645 fa04 807d fc00 741
48bf 0e08 0700 0000 807d ff00 750a c705 48bf 0e08 0700 000
ff00 740f c705 48bf 0e08 fc00 7415 807d ff00 740f c705 48b
0000 00e9 9900 0000 c645 0600 0000 e99e 0000 00e9 9900 000
c645 f900 c645 fa05 807d f701 c645 f800 c645 f900 c645 fa0
fc00 750a c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 750a c705 48bf 0e08 0800 0000 807d fc00 750a c705 48b
fe00 7506 807d ff00 740c 0900 0000 807d fe00 7506 807d ff0
0600 0000 eb4b eb49 c645 c705 48bf 0e08 0600 0000 eb4b eb4
c645 f901 c645 fa02 807d f701 c645 f800 c645 f901 c645 fa0
5dc3 5589 e5c7 0540 bf0e 00b8 5400 0000 5dc3 5589 e5c7 0540
1800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
3000 00b8 4500 0000 5dc3 0540 bf0e 0820 0000 00b8 4500 000
bf0e 0821 0000 00b8 5800 5589 e5c7 0540 bf0e 0821 0000
e5c7 0540 bf0e 0822 0000 0000 5dc3 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec11
3000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 088
8b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08f
30c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
3000 00c9 d901 0000 c645 0548 bf0e 0882 0000 00c9 d901 0000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
18bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
3600 0000 e988 0100 00e9 c705 48bf 0e08 0600 0000 e988 010
  
```

```

4800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
0000 00b8 4500 0000 0000 0820 0000 00b8 4500 0000
bf0e 0821 0000 00b8 5589 e5c7 0812 0000 00b8
e5c7 0540 bf0e 0822 0000 00b8 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec1
0000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 088
8b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08f
00c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
0000 00c9 d901 0000 c645 0548 bf0e 0882 0000 00c9 d901 000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
48bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
0600 0000 e988 0100 00e9 c705 48bf 0e08 0600 e988 010
f701 c645 f800 c645 f900 8001 0000 c645 f701 c645 f800 c64
fc00 740f c705 48bf 0e08 c645 fa02 807d fc00 740f c705 48b
0100 00e9 5901 0000 c645 0400 0000 e95e 0100 00e9 5901 000
c645 f900 c645 fa03 807d f701 c645 f800 c645 f900 c645 fa0
fe00 750a c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 750a c705 48bf 0e08 0500 0000 807d fc00 750a c705 48b
fe00 740f c705 48bf 0e08 0300 0000 807d fe00 740f c705 48b
0100 0000 e988 0100 00e9 c705 48bf 0e08 0600 e988 010
c645 f900 c645 fa03 807d f701 c645 f800 c645 f901 c645 fa0
48bf 0e08 0000 c9c4 f400 c645 f800 c645 f901 c645 fa0
0000 c645 f701 c645 f800 0000 c645 f800 c645 f901 c645 fa0
fa04 807d fc00 7410 807d c645 f900 c645 fa04 807d fc00 741
48bf 0e08 0700 0000 807d ff00 750a c705 48bf 0e08 0700 000
ff00 740f c705 48bf 0e08 fc00 7415 807d ff00 740f c705 48b
0000 00e9 9900 0000 c645 0600 0000 e99e 0000 00e9 9900 000
c645 f900 c645 fa05 807d f701 c645 f800 c645 f900 c645 fa0
fc00 750a c705 48bf 0e08 fd00 7410 807d fe00 750a c705 48b
fc00 750a c705 48bf 0e08 0800 0000 807d fc00 750a c705 48b
fe00 7506 807d ff00 740c 0900 0000 807d fe00 7506 807d ff0
0600 0000 eb4b eb49 c645 c705 48bf 0e08 0600 0000 eb4b eb4
c645 f901 c645 fa02 807d f701 c645 f800 c645 f901 c645 fa0
5dc3 5589 e5c7 0540 bf0e 00b8 5400 0000 5dc3 5589 e5c7 0540
4800 0000 5dc3 5589 e5c7 0812 0000 00b8 4800 0000 5dc3 558
3000 00b8 4500 0000 5dc3 0540 bf0e 0820 0000 00b8 4500 000
bf0e 0821 0000 00b8 5800 5589 e5c7 0540 bf0e 0821 0000
e5c7 0540 bf0e 0822 0000 0000 5dc3 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec11
25c7 0540 bf0e 0822 0000 0000 5dc3 5589 e5c7 0540 bf0e 082
5dc3 5589 e583 ec10 c705 00b8 4900 0000 5dc3 5589 e583 ec11
3000 a148 bf0e 0883 f809 48bf 0e08 0100 0000 a148 bf0e 088
8b04 8548 e10b 08ff e0c6 0f87 0002 0000 8b04 8548 e10b 08f
30c6 45f9 00c6 45fa 00c7 45f7 00c6 45f8 00c6 45f9 00c6 45f
3000 00c9 d901 0000 c645 0548 bf0e 0882 0000 00c9 d901 0000
c645 f900 c645 fa01 807d f701 c645 f800 c645 f900 c645 fa0
18bf 0e08 0300 0000 807d fb00 750a c705 48bf 0e08 0300 000
fc00 750a c705 48bf 0e08 fb00 7410 807d fc00 750a c705 48b
fc00 7415 807d fb00 740f 0900 0000 807d fc00 7415 807d fb0
3600 0000 e988 0100 00e9 c705 48bf 0e08 0600 0000 e988 010
  
```



Guide DSE with an unsound static analysis

CASE 2: reverse & deobfuscation

- Prove something infeasible
- SE cannot help here

eg: $7y^2 - 1 \neq x^2$

(for any value of x, y in modular arithmetic)



```

mov  eax, ds:X
mov  ecx, ds:Y
imul ecx, ecx
imul ecx, 7
sub  ecx, 1
imul eax, eax
cmp  ecx, eax
jz   <dead_addr>
    
```

The predicate is always true

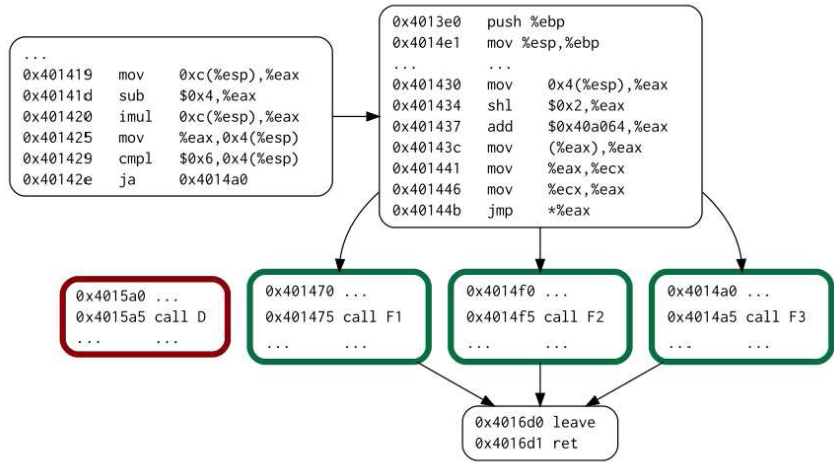
```

if (ax > bx) X = -1;
else X = 1;
    
```

```

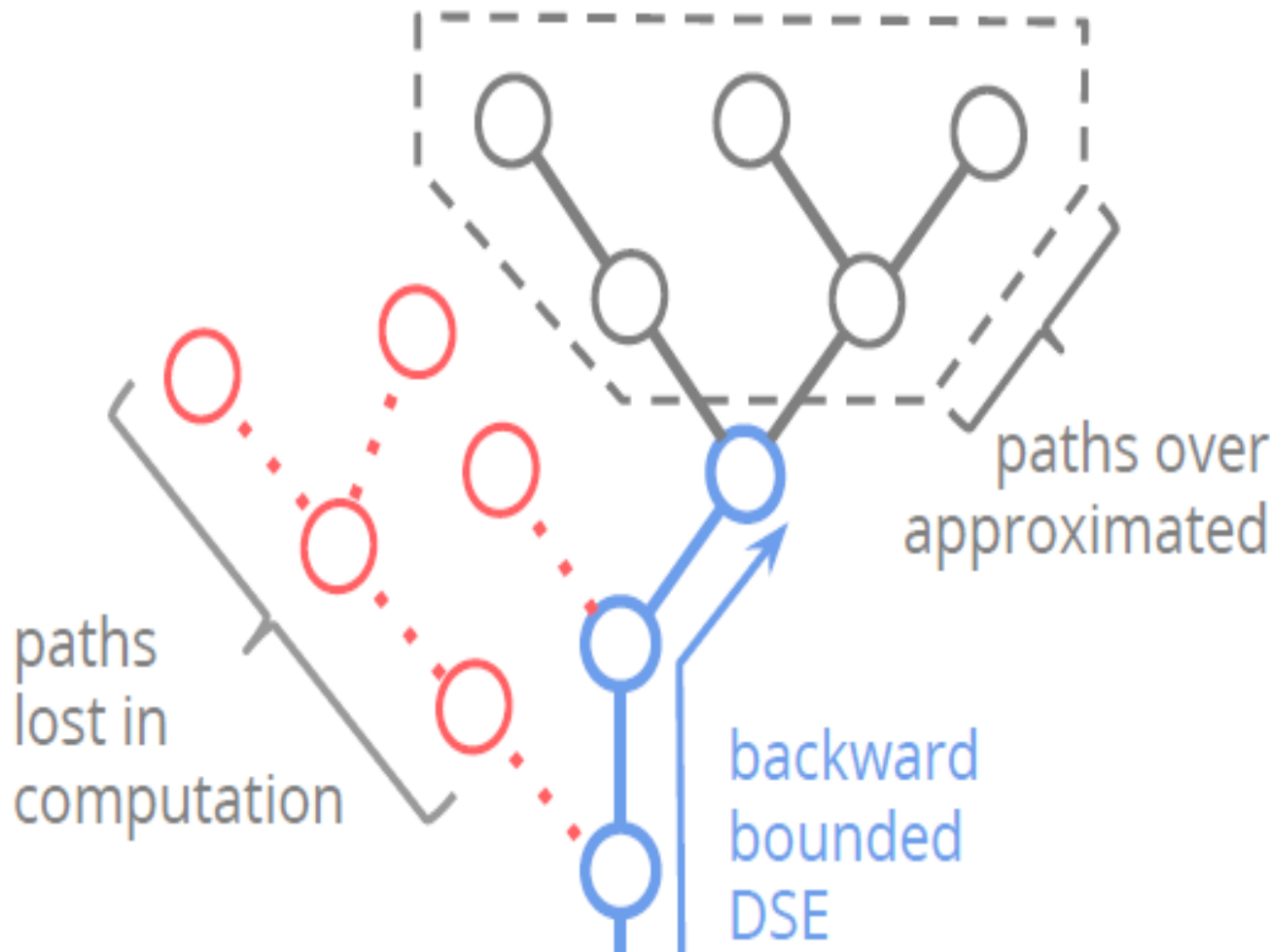
OF := ((ax{31,31}#bx{31,31}) &
      (ax{31,31}#(ax-bx){31,31}));
SF := (ax-bx) < 0;
ZF := (ax-bx) = 0;
if (~ZF ^ (OF = SF)) goto 11
X := 1
goto 12
11: X := -1
12:
    
```

The two blocks are equivalent



With IDA + BINSEC

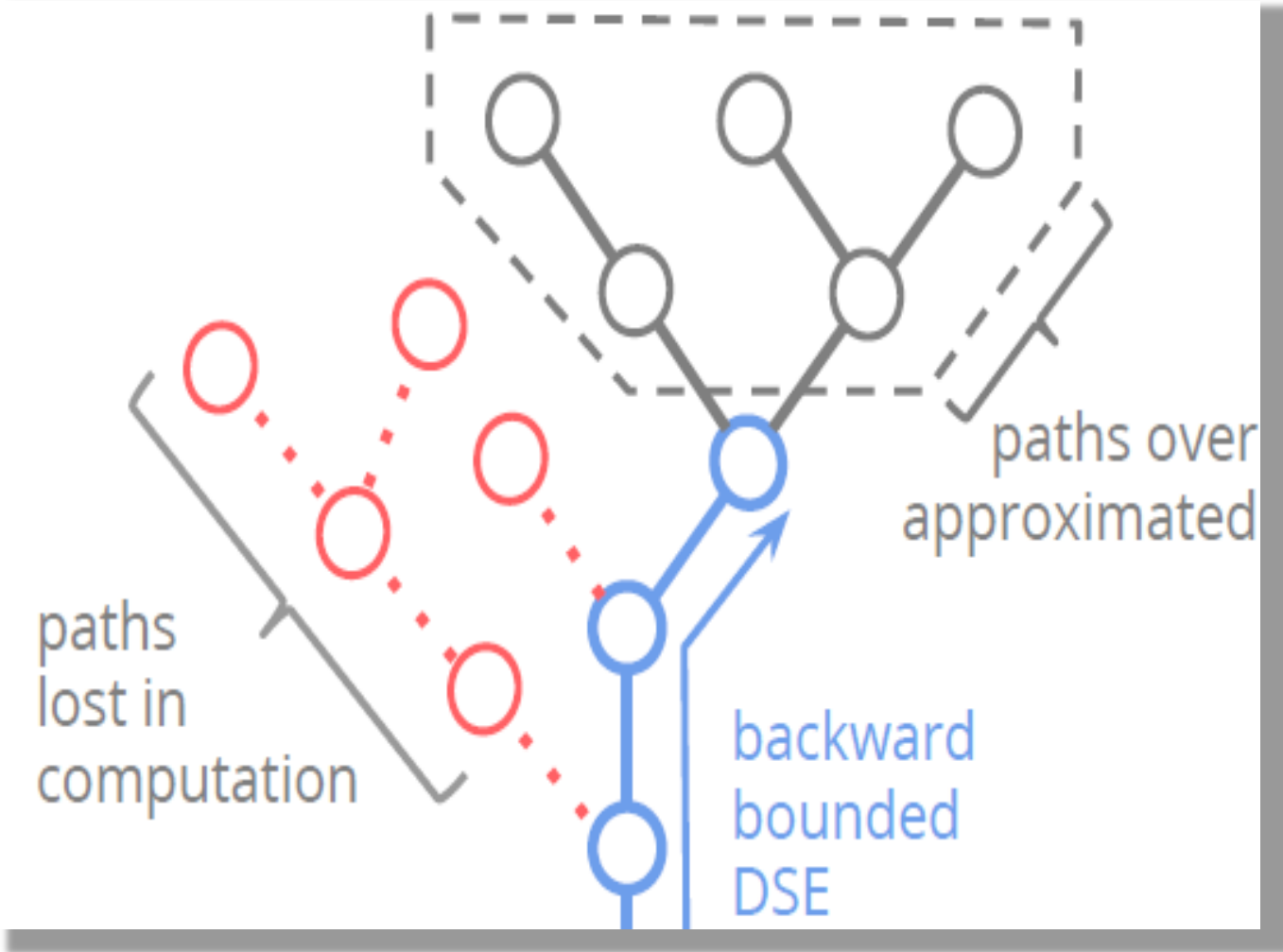
All jump targets are found



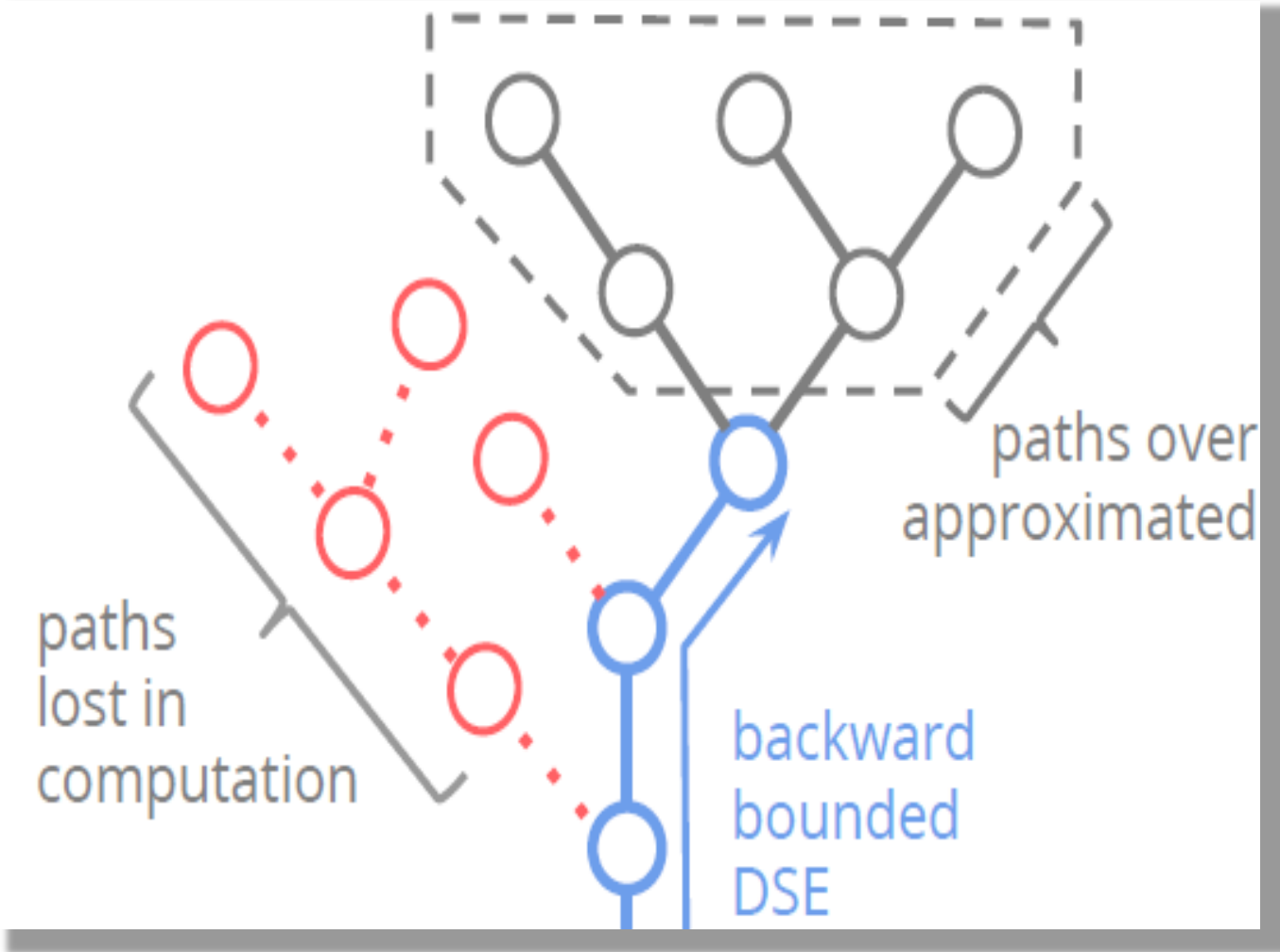
Backward bounded SE

- Compute k-predecessors
- If the set is empty, no pred.
- Allows to **prove** things

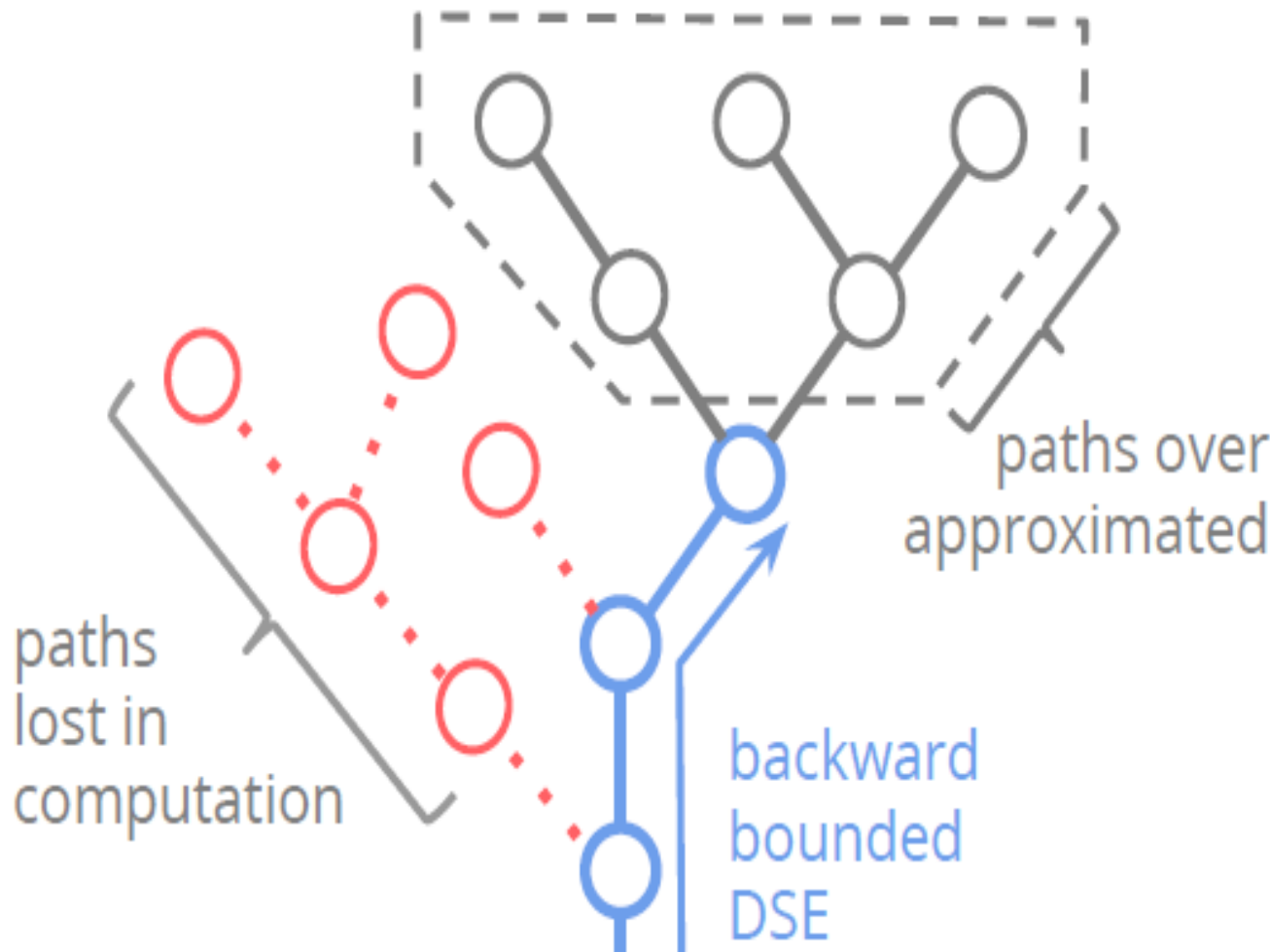
- Prove things
- Local → scalable



- **False Negative: k too small**
 - *Missed proofs*



- **False Negative: k too small**
 - *Missed proofs*
- **False Positive: CFG incomplete**
 - *Wrong proofs ?!*



- **False Negative: k too small**
 - *Missed proofs*
- **False Positive: CFG incomplete**
 - *Wrong proofs*

- Low rate of wrong proofs
- Controlled XPs

Case 2: THE XTUNNEL MALWARE

-- [BlackHat EU 2016, S&P 2017] (Robin David)



X-Agent Spyware

Now Targeting Apple's MacOS Users



Two heavily obfuscated samples

- Many opaque predicates

Goal: detect & remove protections

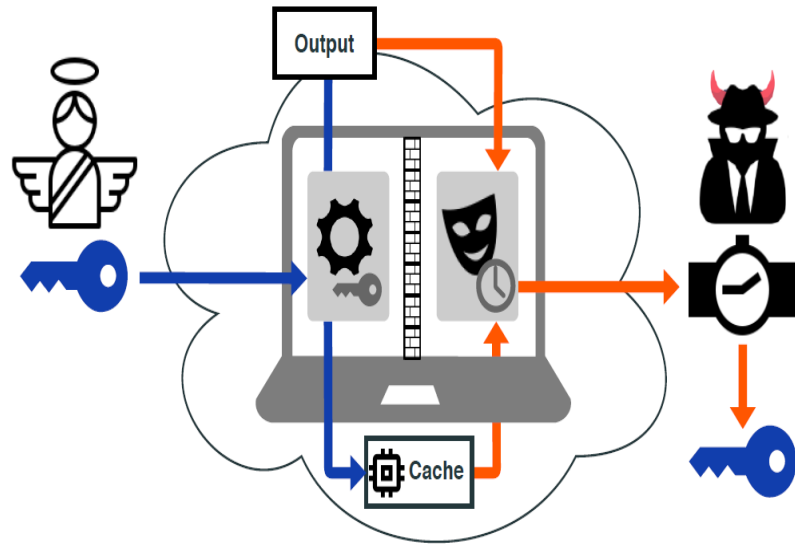
- Identify 40% of code as spurious
- Fully automatic, < 3h [now: 20min]

- ▶ Backward-bounded SE
- ▶ + dynamic analysis

	C637 Sample #1	99B4 Sample #2
#total instruction	505,008	434,143
#alive	+279,483	+241,177

Case 3: SECURING CRYPTO-PRIMITIVES

-- [S&P 2020, NDSS 2021] (Lesly-Ann Daniel)

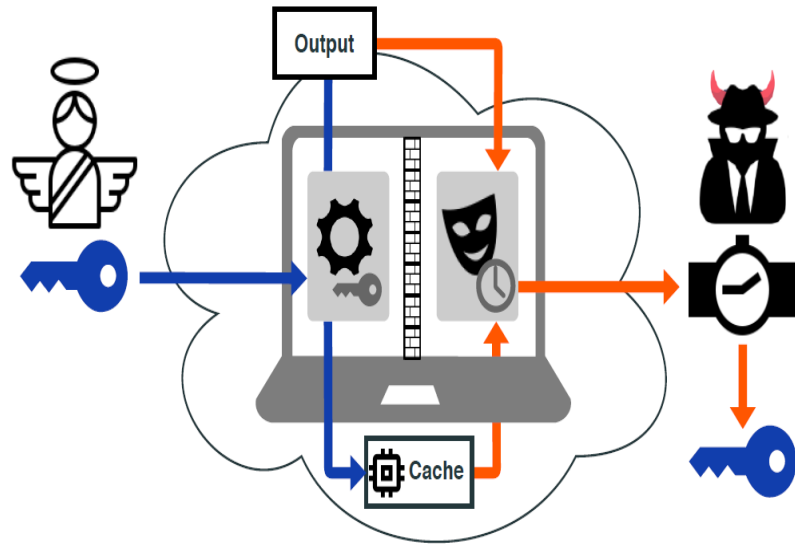


- ▶ Property: timing attacks
- ▶ Attacker: speculation

		#Instr static	#Instr unrol.	Time	CT source	Status	Comment
utility	ct-select	735	767	.29	Y	21×X	21 1 new X
	ct-sort	3600	7513	13.3	Y	18×X	44 2 new X
BearSSL	aes_big	375	873	1574	N	X	32 -
	des_tab	365	10421	9.4	N	X	8 -
OpenSSL	tls-remove-pad-lucky13	950	11372	2574	N	X	5 -
Total		6025	30946	4172	-	42 ×X	110 -

Case 3: SECURING CRYPTO-PRIMITIVES

-- [S&P 2020, NDSS 2021] (Lesly-Ann Daniel)



- ▶ Relational symbolic execution
- ▶ Follows paires of execution
- ▶ Check for divergence
- ▶ Sharing, merging, preprocess

		#Instr static	#Instr unrol.	Time	CT source	Status	Comment
utility	ct-select	735	767	.29	Y	21 x X	21 1 new X
	ct-sort	3600	7513	13.3	Y	18 x X	44 2 new X
BearSSL	aes_big	375	873	1574	N	X	32 -
	des_tab	365	10421	9.4	N	X	8 -
OpenSSL							
	tls-remove-pad-lucky13	950	11372	2574	N	X	5 -
Total		6025	30946	4172	-	42 x X	110 -

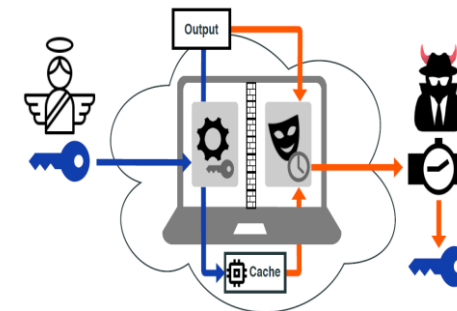
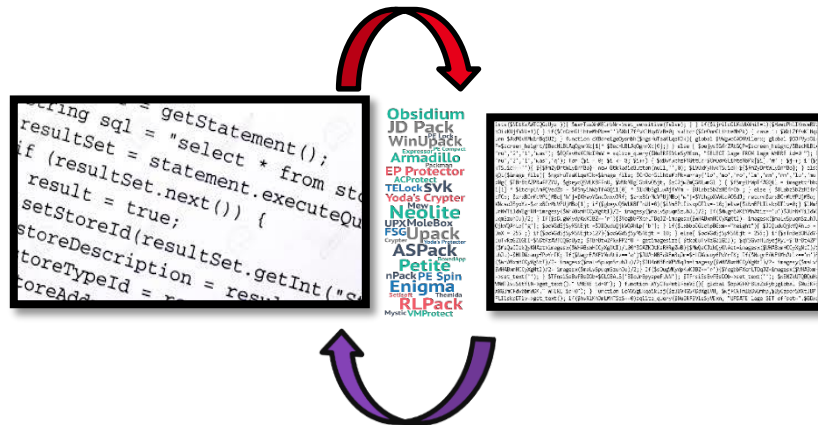
- 397 crypto code samples, x86 and ARM
- New proofs, 3 new bugs (of verified codes)
- Potential issues in some protection schemes
- 600x faster than prior work!

Under the hood: finely tune the technology



- SMT solvers are powerful weapons
- But (binary-level) security problems are terrific beasts

- **Finely tuning the technology can make a huge difference**

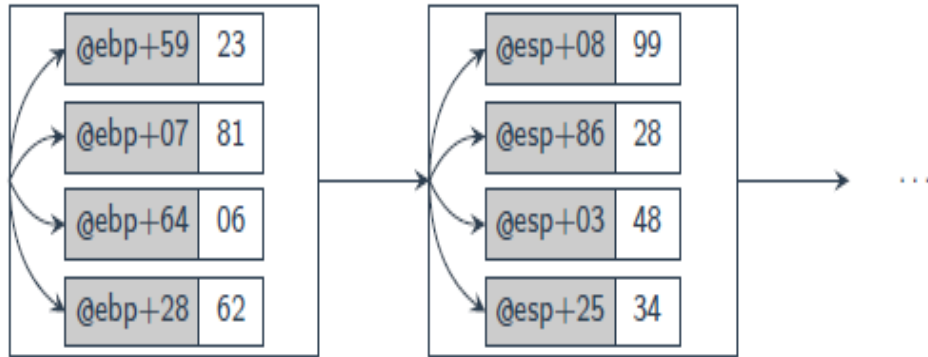


• Some queries: 24h → 1min

• 600x faster than prior approach

Tuning the solver: intensive array formulas [LPAR 2018] (Benjamin Farinier)

- **Makes the difference!**

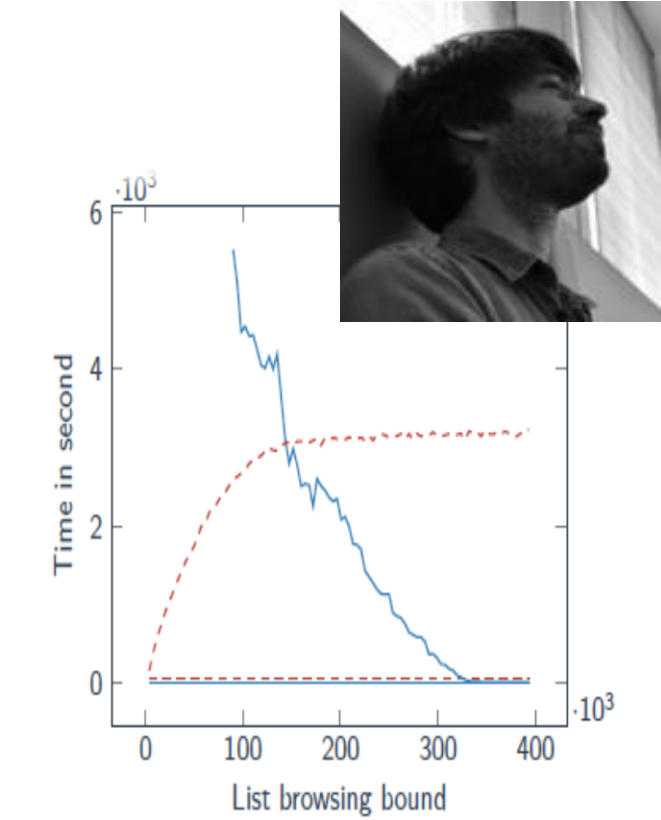


- Dedicated data structure (list-map)
- Tuned for base+offset access
- Linear complexity

- Huge formula obtained by dynamic symbolic execution
- 293 000 select
- **24 hours of resolution!**

Using LMBN

- #select reduced to 2467
- 14 sec for resolution
- 61 sec for preprocessing



Using list representation

- Same result with a bound of 385 024 and beyond...
- ...but 53 min preprocessing

Array theory

- Necessary to model memory
- Hard for solvers (case splits)

- Reading in a at index $i \in \mathcal{I}$: $\text{select } a \ i$
- Writing in a an element $e \in \mathcal{E}$ at index $i \in \mathcal{I}$: $\text{store } a \ i \ e$

$$\text{select} : \text{Array } \mathcal{I} \ \mathcal{E} \rightarrow \mathcal{I} \rightarrow \mathcal{E}$$

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$$\forall a \ i \ e. \text{select} (\text{store } a \ i \ e) \ i = e$$

$$\forall a \ i \ j \ e. (i \neq j) \Rightarrow \text{select} (\text{store } a \ i \ e) \ j = \text{select } a \ j$$

ROW rule may
introduce case-splits

Prevalent in software analysis

- Modelling memory
- Abstracting data structure
(map, queue, stack...)

Hard to solve

- NP-complete
- ROW may require case-splits

Goal: make it tractable

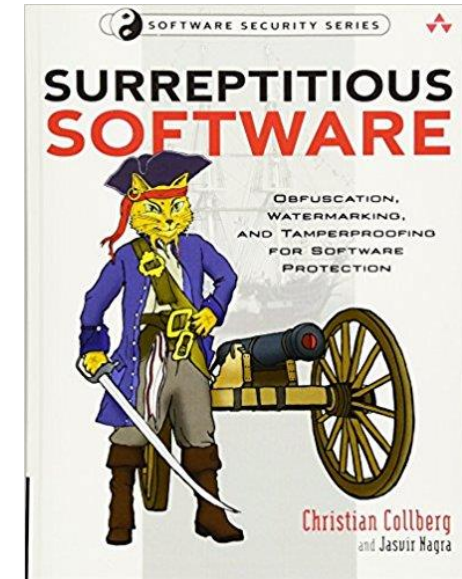
Not pure theory!

Reverse of a ASPACK-protected code

Huge formula obtained by dynamic symbolic execution

293 000 select

24 hours of resolution!



```
...
  sql = getStatement();
  resultSet = statement.executeQuery(sql);
  if (resultSet.next()) {
    result = true;
    setStoreId(resultSet.getInt("storeDescription = resultStoreId = r
    storeAd=
  }
}
```

```
lists ($MDeKaMTCQgUlyz ) { $marTuzXwEiMbr~set_sensitive(false); } ...
  sql = getStatement();
  resultSet = statement.executeQuery(sql);
  if (resultSet.next()) {
    result = true;
    setStoreId(resultSet.getInt("storeDescription = resultStoreId = r
    storeAd=
  }
}
```

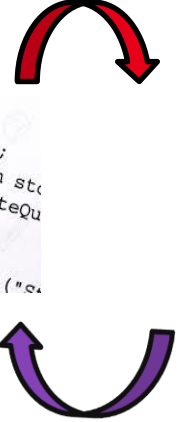
- Obsidium
- JD Pack
- WinUpack
- Expressor
- PE Compact
- Armadillo
- Packman
- EP Protector
- ACProtect
- TELockSVK
- Yoda's Crypter
- Mew
- Neolite
- UPX MoleBox
- FSGUpack
- Crypter
- Yoda's Protector
- ASPack
- BoxedApp
- Petite
- nPack
- PE Spin
- Enigma
- Themida
- Setisoft
- RLPack
- Mystic
- VMProtect

Not pure theory!

Reverse of a ASPACK-protected code

```

        - = getStatement();
        resultSet = "select * from stu
        if (resultSet = statement.executeQu
        result = true;
        setStoreId(resultSet.getInt("s
        storeDescription = resu
        storeTypeId = r
        storeAdr
    
```



```

lists ($MdxKaMTQGQlyz }) ($mTuZwMElbnR->set_sensitive(False); ) if ($!jllGLMcMxMll+1)($!HexPILkmsbYK
BOLIKUJfWml=1) { if ($!OorGLlhtemPke=="")$!KLZFfVKHqYzBq; switch ($!OorGLlhtemPke) { case 1: $!KLZFfVKHq
um $!GoWmLlrbSuz; } function c0b0w0lq0ymh ($!gthTmKlq0ymh) { global $!mpg03WmlLenz; global $!Olylq0
P-;screen_height;$!redHLlLAcDqmk[1]* $!redHLlLAcDqmk[0]; } else { $!ojsySGrfZAGQP-;screen_height;$!redHLlL
"ru","z","l","was","q"; for ($! = 0; $! < 8; $!++) { $!BvWchzPffTted-$!OorGLlhtemPke[1].H ; $!++; if ($
kISulohm+"") { ($!Byb0mThyJmBo) = new GetRadLobction (null,"",0); $!Wu0mWkISulohm ($!Byb0mThyJmBo); } elst
gQ ($!Image_File) ($!gthTmKlq0ymh;$!Image_File;$!OorGLlhtemPke+""+"l";"m";"l";"m";"m";"l";"m");
dli ($!B-0LzPwFPZYU; $!qbeyoCSILKBFfFru; $!WmMgGtGRVCSjz; $!zUwzGGLueLd) ($!SmylMqTfAQ011 = ImagetFrb
l(1) * $!tchP0Umq0vedo - $!SmylMqTfAQ011[0] * $!lHb0gluaAJfvfm - $!lLabszSzHEfrcb; } else { $!lLabszSzHEfrc
cFco; $!zr0CrMcVPUjYBBo[ "h"-;$!kHevGncDaxw37R; $!zr0CrMcVPUjYBBo[ "w"-;$!YUqoKvMLA0Gd; return $!zr0CrMcVPUjYBBo;
WlcadZyetz-$!zr0CrMcVPUjYBBo[1]; if ($!qbeyoCSILKBFfFru=0) {$!mPCLlLskpTLv=10; } else {$!mPCLlLskpTLv=0; } $!lM
0WnTlS0vghm=Imagex ($!WABmhCCoXglt1)/2- Imagex ($!alVSpuqSzuhU)/2; if ($!MgREKEYWAlz="") {$!MgREKEYWAlz=$!alVSpuqSzuhU
0vSpZuhU)/2; } if ($!DugMkydKwKlBZ="") {$!ogtPkrLTDz2=Imagex ($!WABmhCCoXglt1) - Imagex ($!alVSpuqSzuhU
Q3kVqHlPlg"); $!o0Gd555MSMEjz-$!lQudUQ3kVqHlPlg"); } if ($!Lbb030u0qB0om="height") { $!lQudUQ3kVqHlPlg =
DmK = 255; } if ($!o0Gd555MSMEjz>127) {$!o0Gd555MSMEjz = 10; } else { $!o0Gd555MSMEjz = 255; } if ($!Treb0z0z0F
EufWkZlGfI-$!MdxKaMTQGQlyz; $!B-0LzPwFPZYU = getImagesze ($!c0b0w0lq0ymh); $!J50wW0lyeJmJl-$!Treb0z0z0F
($!WqCz32q0WkLzImagex ($!WABmhCCoXglt1)/4R0*;$!QKZC0K0hR0q0B) ($!MgREKEYWAlz=Imagex ($!WABmhCCoXglt1);
u0u) -;$!LDX0xuyPofrFk; if ($!MgREKEYWAlz="") {$!U0wME0KvWlqJm=Imagex ($!WABmhCCoXglt1)/2- Imagex ($!alV
($!WABmhCCoXglt1)/2- Imagex ($!alVSpuqSzuhU)/2; } $!U0wME0KvWlqJm=Imagex ($!WABmhCCoXglt1)/2- Imagex ($!alV
($!WABmhCCoXglt1)/2- Imagex ($!alVSpuqSzuhU)/2; } if ($!DugMkydKwKlBZ="") {$!ogtPkrLTDz2=Imagex ($!WABmh
->set_text (""); } $!FndLs0vB0300-$!GL0AL [$!BldU0v0v0vFlm]; } $!FndLs0vB0300->set_text (""); } $!MCHDU0B04H
WnTLv0StfFlm-;get_text (); } function XyCTUPrcFeME ( $ global $!oAGFRHlZzYfy0;global $!UzERF
Xl0GwF0v0b0Mk." WHERE Id=0"; } function EoNv0g0k0kLzj ($!ZBR0vGSDx0gELW; $!JfCRfmlB0v0mp;$!ofz0srSMT3DPl
PLlLskpTLv->get_text (); if ($!WkLk0mLmHtS==0) {$!qlite_query ($!UERFSVle5yEz0n; "UPDATE Lage SET ofise=""-$!Gw
    
```

Huge formula
dynamic symb
293 000 select

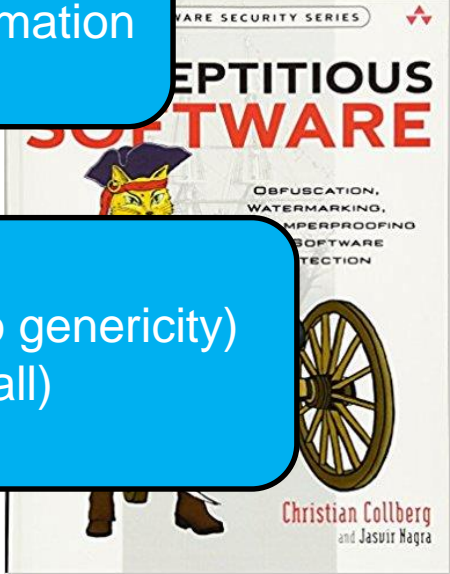
Remember: binary-level

- Very long chains of write
- A single memory, no partition information

Sad state-of-the-art:

- concretize memory accesses (scale, no genericity)
- Keep symbolic (generic but no scale at all)

24 hours



Inner-working of array theory

- Reading in a at index $i \in \mathcal{I}$: $\text{select } a \ i$
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« Logical arrays » as chains of store
(« list representation »)

ROW reasoning may
introduce case-splits

Eliminate ROW



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ROW rules could be used
as a preprocessing??



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« Logical arrays » as chains of store
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ROW reasoning may introduce case-splits

Eliminate ROW

ROW rules could be used as a preprocessing??

Quadratic reasoning

- Term-based equality
- Disequality??

- Constant case: too slow
- Symbolic case: no simplif.

Inner-working of array theory

« Logical arrays » as chains of store
(« list representation »)

• Reading in a at index $i \in \mathcal{I}$: $\text{select } a \ i$
 • Writing in a an element e at index $i \in \mathcal{I}$: $\text{store } a \ i \ e$

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Goal: efficient preprocessing to remove ROW

- Completely address the constant case
 - Help for the symbolic case
 - Go beyond ROW (eg, WOW)

ing may
se-splits

Eliminate ROW

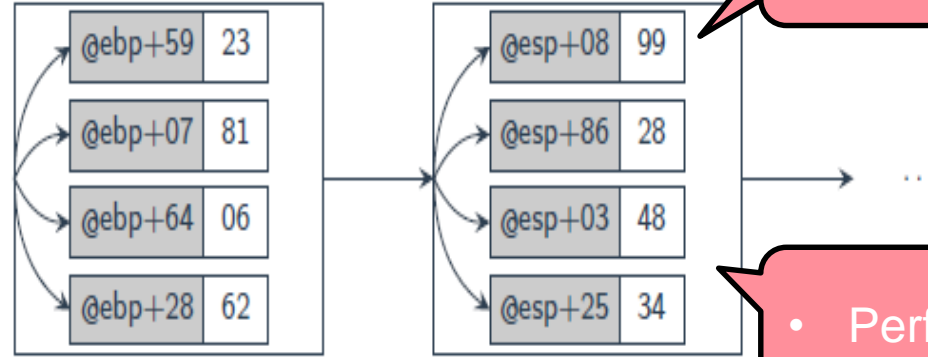
ROW rules could be used
as a preprocessing??

Quadratic reasoning

- Term-based equality
- Disequality??

Fast array simplification (1)

- Dedicated data structure (list-map)
- Tuned for **base+offset** access
- **Base** can be symbolic
- $n * \ln(n)$ complexity



- Scale
- Good when only few bases

- Perfect for constant case

Still limited by term-equality reasoning

Fast array simplification (2)

- Dedicated data structure (list-map)
- Tuned for **base+offset** access
- **Base** can be symbolic
- $n * \ln(n)$ complexity



- Scale
- Good when only few bases

Propagate "variable+constant" terms

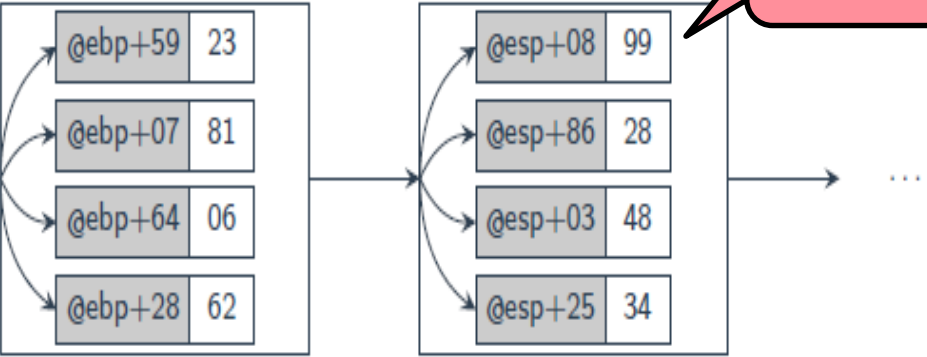
- If $y \triangleq z + 1$ then $x \triangleq y + 2 \rightsquigarrow x \triangleq z + 3$
- Together with associativity, commutativity...

Still limited by disequality reasoning

- Reduce the number of bases
- Perfect for symb. stack over simple functions

Fast Array Simplification

- Dedicated data structure (list-map)
- Tuned for **base+offset** access
- **Base** can be symbolic
- $n * \ln(n)$ complexity



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Propagate “variable+constant” terms

- If $y \triangleq z + 1$ then $x \triangleq y + 2 \rightsquigarrow x \triangleq z + 3$
- Together with associativity, commutativity...

- Prove disequalities between different bases

- Reduce the number of bases
- Perfect for symb. stack over simple functions

Associate to every indices i an abstract domain $i^\#$

- If $i^\# \sqcap j^\# = \perp$ then $(a[i] \leftarrow e)[j] = a[j]$
- Integrated in the list-map representation

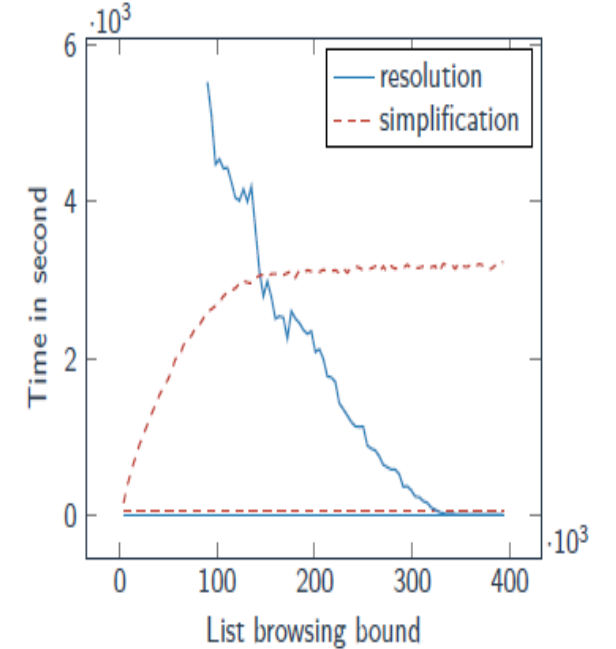
- Excellent for DSE-like formulas
- Slight overall improvement over SMTCOMP

no block cypher	#select		
	Z3	all arrays	non initial
no simplification	0 606.7	1448301	1448001
list-16	0 501.0	1075358	1052786
list-256	0 371.9	807778	762673
map	0 370.5	807778	762673
LMBN	0 46.0	65788	5044

- Huge formula obtained by dynamic symbolic execution
- 293 000 select
- 24 hours of resolution !

Using LMBN

- #select reduced to 2467
- 14 sec for resolution
- 61 sec for preprocessing



Using list representation

- Same result with a bound of 385 024 and beyond...
- ...but 53 min preprocessing



Fresh results



No Crash, No Exploit: Automated Verification of Embedded Kernels

Olivier Nicole*†, Matthieu Lemerre*, Sébastien Bardin* and Xavier Rival‡

*Université Paris-Saclay, CEA List, Saclay, France

†Département d'informatique de l'ENS, ENS, CNRS, PSL University, Paris, France

‡Inria, Paris, France



olivier.nicole@cea.fr, matthieu.lemerre@cea.fr, sebastien.bardin@cea.fr, xavier.rival@ens.fr

Abstract—The kernel is the most safety- and security-critical component of many computer systems, as the most severe bugs lead to complete system crash or exploit. It is thus desirable to guarantee that a kernel is free from these bugs using formal methods, but the high cost and expertise required to do so are deterrent to wide applicability. We propose a method that can verify both *absence of runtime errors* (i.e. crashes) and *absence of privilege escalation* (i.e. exploits) in embedded kernels from their binary executables. The method can verify the kernel runtime

system developers only provide their code and, with very little configuration or none at all, the tool automatically verifies the properties of interest. In addition, a comprehensive verification should carry to the binary executable, as 1. a large part of embedded kernel code consists in low-level interaction with the hardware, and 2. the compilation toolchain (build options, compiler, assembler, linker) may introduce bugs [12].

Recent so-called “push-button” kernel verification methods [13]–[15] are based on symbolic execution [16]–[18] which

- Full verification of embedded kernels
- RTAS 2021 (best paper award)

Not All Bugs Are Created Equal, But Robust Reachability Can Tell The Difference

Guillaume Girol¹, Benjamin Farinier², and Sébastien Bardin¹

¹ Université Paris-Saclay, CEA, List, France first.last@cea.fr

² TU Wien, Vienna, Austria first.last@tuwien.ac.at



Abstract. This paper introduces a new property called *robust reachability* which refines the standard notion of reachability in order to take replicability into account. A bug is robustly reachable if a *controlled input* can make it so the bug is reached whatever the value of *uncontrolled input*. Robust reachability is better suited than standard reachability in many realistic situations related to security (e.g., criticality assessment or bug prioritization) or software engineering (e.g., replicable test suites and

- Focus on robust bugs
- CAV 2021

Example 2: robust symbolic execution [CAV 2018, CAV 2021]

- **Standard symbolic reasoning** may produce **false positive**

What?!!

Safety is not security ...

- **for example here:**
 - SE will try to solve $a * x + b > 0$
 - May return $a = -100, b = 10, x = 0$
- **Problem: x is not controlled by the user**
 - If x change, possibly not a solution anymore
 - Example: $(a = -100, b = 10, x = 1)$

In practice: canaries, secret key in uninitialized memory, etc.

```
int main () {
    int a = input ();
    int b = input ();

    int x = rand ();

    if (a * x + b > 0) {
        analyze_me();
    }
    else {
        ...
    }
}
```

Example 2: robust symbolic execution

- Standard symbolic reasoning may produce **false positive**

- Actually, need to solve $\forall x. ax + b > 0$

- How to solve it? (CAV18)

- Robust reachability (CAV'21)

```
int main () {
    int a = input ();
    int b = input ();

    int x = rand ();

    if (a * x + b > 0) {
        analyze_me();
    }
    else {
        ...
    }
}
```

Our solution: reduce quantified formula to the quantifier-free case

- Approximation
- But reuse the whole SMT machinery

Key insights:

- independence conditions
- formula strengthening

- Quantified reachability condition

① $\forall x. ax + b > 0$

- Taint variable constraint

② $a^* \wedge b^* \wedge \neg x^*$ (a^*, b^*, x^* : fresh boolean variables)

- Independence condition

③ $((a^* \wedge x^*) \vee (a^* \wedge a = 0) \vee (x^* \wedge x = 0)) \wedge b^*$

④ $((\top \wedge \perp) \vee (\top \wedge a = 0) \vee (\perp \wedge x = 0)) \wedge \top$

⑤ $a = 0$

- Quantifier-free reachability condition

⑥ $(ax + b > 0) \wedge (a = 0)$

- **Context: a little bit of formal methods for safety**
- **Binary-level security analysis: benefits & challenges**
- **The BINSEC platform**
- **From source-level safety to binary-level security: some examples**
- **Conclusions**

SOME KEY PRINCIPLES BEHIND OUR WORK?

- **Robustness & precision are essential**
 - DSE is a good starting point
 - dedicated robust and precise (but not sound) static analysis are feasible
- **Can be adapted beyond the basic reachability case**
 - variants (backward, relational, robust)
 - combination with other techniques
- **Loss of guarantees**
 - Accept ... But control!
 - Look for « correct enough » solutions
- **Finely tune the technology**
 - Tools for safety are not fully adequate for security

Conclusion

- **Security is not safety, and it's great fun for FM/PL researchers**
 - Binary level, attacker model, true security properties
- **Need to revisit (deeply?) standard methods**
 - Two different stories: Symbolic Execution vs. Static Analysis
 - Variants, combinations
- **Need a real « security-oriented » code analysis framework**
- **Some results in that direction, still many exciting challenges**

BINSEC is available (new release)

<https://binsec.github.io>

ANR Project TAVA

Looking for PhD & postdoc

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Software & Systems Engineering Department
List, CEA Tech

Florent Kirchner
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