



CISPA



Schrodinger's Squirrel

Formal security proofs in a post-quantum world

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CISPA Helmholtz Center for Information Security

November 19, 2021

Formal Methods for Security and Privacy

The beautiful and frightening technological revolution



It's my life!



The beautiful and frightening technological revolution



The beautiful and frightening technological revolution



The beautiful and frightening technological revolution



The beautiful and frightening technological revolution



The beautiful and frightening technological revolution



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The beautiful and frightening technological revolution



Sacrifice privacy in exchange of services...

The beautiful and frightening technological revolution



Sacrifice privacy in exchange of services...

The beautiful and frightening technological revolution



Sacrifice privacy in exchange of services...

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Sacrifice privacy in exchange of services...
but our data is used against us!

Some people even need privacy to **survive**:

- Reporters in dangerous countries.
- Homosexual in countries where it is punished by law (still 69 in the world...).
- Uighurs tracked through their smartphones in China.

If we can't have privacy, **nobody** can

Security and Privacy Matter !

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We need:

- systems **designed** to provide security and privacy;

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- with **guarantees** that they do;

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We need:

- systems **designed** to provide security and privacy;
- with **guarantees** that they do;
- **used** in practice.

The (first) difficulty

Protocols



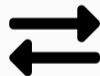
SSH
TLS
GPG
...

The (first) difficulty

Primitives

Protocols

X^1



RSA
Elliptic curves
...

SSH
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...

The (first) difficulty

Implementation

Primitives

Protocols



C++
Java
Python
...

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OS

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Hardware



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Hardware



OS



Implementation



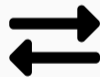
C++
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Primitives



RSA
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Protocols



SSH
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Users



The (first) difficulty

If any link of the chain is broken, everything is.

Hardware

OS

Implementation

Primitives

Protocols

Users



C++
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RSA
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The (first) difficulty

Hardware

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Since the 80's

Provide guarantees on the protocol assuming that the other layers are secure.

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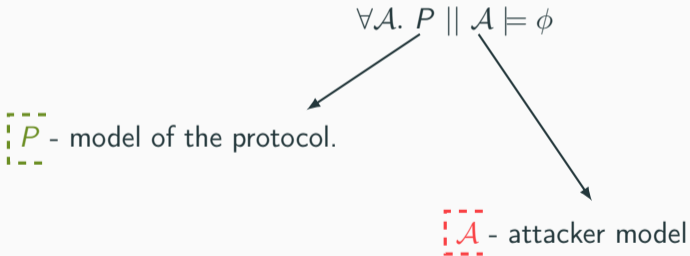
P - model of the protocol.

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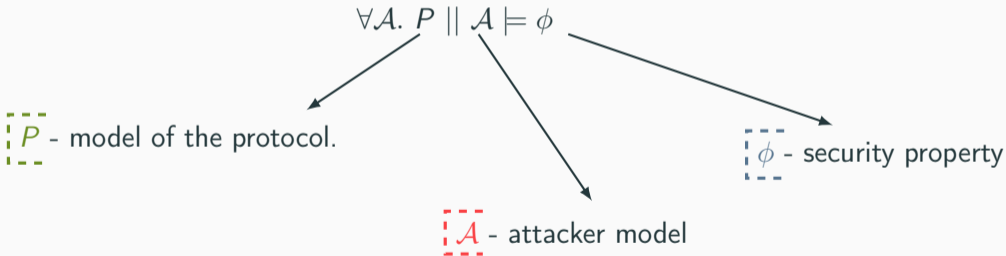


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Attacker Model

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Computation Model

- Turing Machines or inference rules
- Assumptions on primitives (RSA)
- Timing attacks

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Protocol Model

- Optional behaviours or parameters
- Modeling of parsing, serialization
- Communications channels

Second Difficulty - The modeling

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Security Properties

- Secrecy, PFS, PCS
- Authentication
- Unlinkability

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Strong guarantees

Get proofs of security, with all modelings as **realistic** as possible.

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Get proofs of security, with all modelings as **realistic** as possible.

It is very very very very very difficult

We want to prove over realistic models that something is **impossible**, even when considering **all possible** attackers.

- Undecidable;
- complexity of proofs grows very quickly, and cannot be managed by hand.

Computer-Aided Cryptography (since 2000)

Tools that help us carry-out, **verify or automate** the proofs.

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Tools that help us carry-out, **verify or automate** the proofs.

But...

- Inherent **trade-off** between the realism and automation/proof-size;
- no single tool will be the best at everything.

The landscape of computer-aided cryptography

Symbolic Tools

Computational Tools

The landscape of computer-aided cryptography

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(Proverif, Tamarin, Deepsec, ...)

Computational Tools

(EasyCrypt, CryptoVerif, Squirrel ...)

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Attacker

Fixed set of computations

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Turing Machines

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Attacker
Compromise

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Many

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Turing Machines
Few

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Core parts in isolation

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State of the art

- Many tools used **successfully**, both to prove security or discover new vulnerabilities on complex systems.

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State of the art

- Many tools used **successfully**, both to prove security or discover new vulnerabilities on complex systems.
- Still many **limitations**, and still very difficult to work on realistic models.

What I have been doing

Theory - Make proofs easier for realistic models

Practice - Actually make proofs for realistic models

What I have been doing

Theory - Make proofs easier for realistic models

- Composition results to cut computational and symbolic proofs into **modular** pieces;
[Comon, J., Scerri - CCS'20]

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6000 scenarios generated and verified in 5 minutes [Kremer, J. - CSF'18, TOPS]

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Practice - Actually make proofs for realistic models

- **Extensive** analysis in Proverif of multi-factor authentication;
6000 scenarios generated and verified in 5 minutes [Kremer, J. - CSF'18, TOPS]
- Modular analysis of **SSH** in Squirrel, with optional feature of agent forwarding;
Carried out first in the composition paper and then in the Squirrel one.

Today's presentation

A new attacker model

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- What changes with a quantum attackers?
- Can tools already provide guarantees about them?
- If not, what can we do to fix them?

**What is the fuss about quantum
attackers?**

When?

No scaling quantum computers

When?

No scaling quantum computers *yet...*

When?

No scaling quantum computers **yet. . .**

The issue

Quantum computers allow for a **significant speed up** for solving many problems
⇒ breaks RSA, computes discrete logarithms. . .

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Quantum computers allow for a **significant speed up** for solving many problems
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↔ We need new **primitives**, new **protocols** and new **proofs**.

Symbolic Tools

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Attacker Fixed set of possible computations
on abstract messages

Computational Tools

(EasyCrypt, CryptoVerif, ...)

Turing Machines
on bitstrings

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Post-quantum? Abstract reasoning still valid

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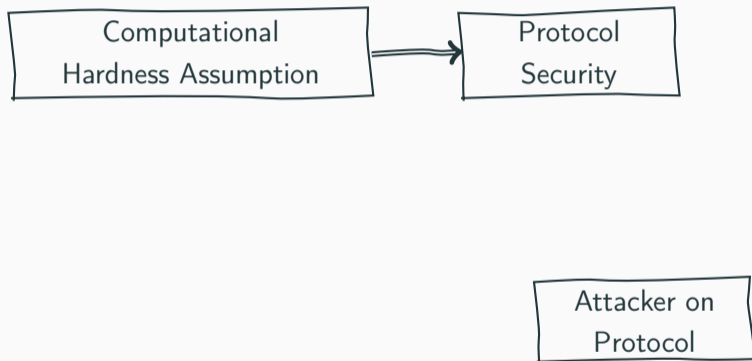
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Quantum Turing Machines

A first look at classical computational proofs



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Two ingredients

- An assumption

(a computational assumption that holds for any attacker, e.g. RSA is unbreakable)

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(the construction of a new attacker using the one against the assumption,
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A tale of two issues

- No drop in quantum replacement for some classical assumptions (DDH).
- There are ways to manipulate a classical attacker that **cannot be done** with a quantum one.

What is a classical attacker?

Probabilistic attacker model

A deterministic computer \mathcal{A} with a random string ρ and inputs \vec{i}

$$\mathcal{A}(\rho, \vec{i})$$

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Allows to simulate weird executions

Run twice the attacker with the **same source** of randomness on **two distinct** inputs:

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Impossible computation with a quantum computer

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↔ Reductions must not use techniques relying on this (e.g., rewinding)

Many pitfalls

Must be careful about

- manipulations of the attacker's state;
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↔ The computational tools do this kind of things. . .

Our contributions¹

¹Joint work with Cas Cremers, Caroline Fontaine, and discussions with Hubert Comon.

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- Take the **BC logic** - a logic for deriving computational security guarantees

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- Take the **BC logic** - a logic for deriving computational security guarantees
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- Take the **Squirrel Prover** - an interactive prover for the BC logic
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- Use it on some new protocols - KEM based post-quantum key exchanges

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Some related work

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- EasyPQC - [BBFGHKSWZ - CCS'21] (parallel work)
 - ↪ Post-quantum sound EasyCrypt - hard to scale to protocols

A post-quantum BC logic

The BC logic

The BC logic²

A **first-order logic** to prove the security of protocols.

²[Bana,Comon-CCS'14]

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A computationally sound logic

Three main ingredients:

- terms, and their **interpretation** so that terms can syntactically describe all behaviours of a protocol;
 - ↪ if there exists an attack on the protocol, we can see it on the terms.

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 - ↪ if there exists an attack on the protocol, we can see it on the terms.
- logical **predicates and rules** (with axioms about e.g. RSA) to reason over the terms;
- prove the **soundness** of the rules, i.e., they correspond to valid reduction.
 - ↪ if there is an attack on the protocol, there is an attack against the axioms.

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Make it post-quantum sound

- New primitives;
 ↪ design new axioms and rules.

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 - ↪ design new axioms and rules.
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 - ↪ do we manipulate the attacker in a bad way?

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 \hookrightarrow design new axioms and rules.
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- Verify the term interpretation;
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Make it post-quantum sound

- New primitives;
 - ↪ design new axioms and rules. **straightforward**
- Verify the post-quantum soundness of the rules;
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- Verify the term interpretation;
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Make it post-quantum sound

- New primitives;
 - ↪ design new axioms and rules. straightforward
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- Verify the term interpretation;
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Make it post-quantum sound

- New primitives;
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- Verify the post-quantum soundness of the rules;
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- Verify the term interpretation;
↪ do we manipulate the attacker in a bad way? Yes

The BC logic³

³[Bana,Comon-CCS'14]

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Protocols are now expressed only with **terms**, i.e., purely syntactic construct, where everything becomes pure functional calls.

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BC terms

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$$sk \stackrel{\$}{\leftarrow} \{0, 1\}^\eta$$

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Classical proofs	BC terms
$sk \stackrel{\$}{\leftarrow} \{0, 1\}^\eta$	sk
$m \stackrel{\$}{\leftarrow} \mathcal{A}(1^\eta)$	

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Classical proofs

$$sk \stackrel{\$}{\leftarrow} \{0, 1\}^\eta$$

$$m \stackrel{\$}{\leftarrow} \mathcal{A}(1^\eta)$$

$$t \stackrel{\$}{\leftarrow} \text{enc}(m, sk)$$

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enc(att₀(), r, sk)

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att₁(enc(att₀(), r, sk))

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From protocols to terms

A protocol

```
new sk;  
in(x);  
if  $x = sk$  then  
  out(ko)  
else  
  out(ok)
```

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new sk;  
in(x);  
if x = sk then  
  out(ko)  
else  
  out(ok)
```

Becomes a term

```
if (att0() = sk) then ko else ok
```

Some rules

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Refl

$$\frac{}{u \sim u}$$

Some rules

Refl

$$\frac{}{u \sim u}$$

=ind

$$\frac{}{(t \doteq n) \sim \text{false}}$$
 when n does
not occur in t

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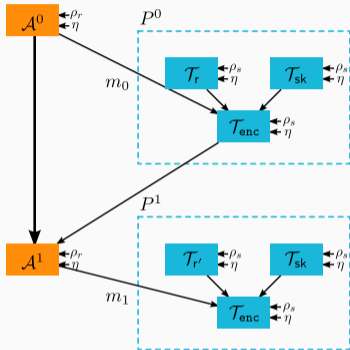
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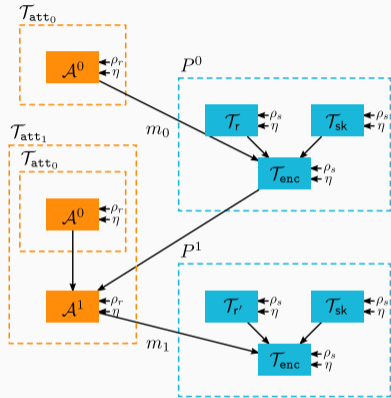
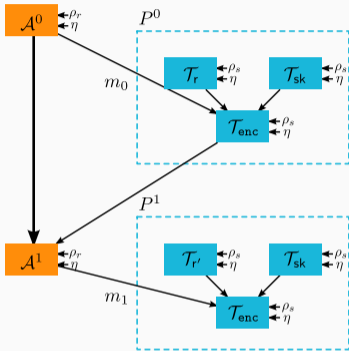
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↪ Solved by specifying that $\mathcal{T}_{\text{att}_1}$ always starts by recomputing the state of $\mathcal{T}_{\text{att}_0}$

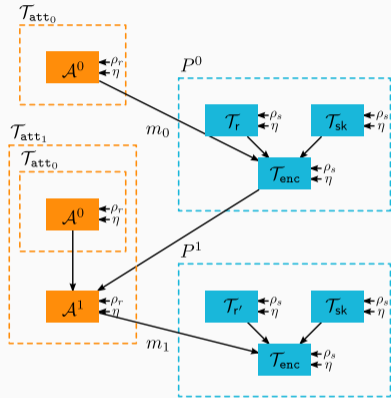
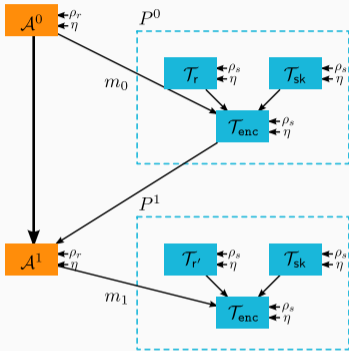
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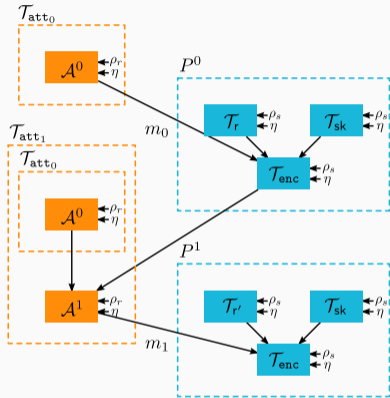
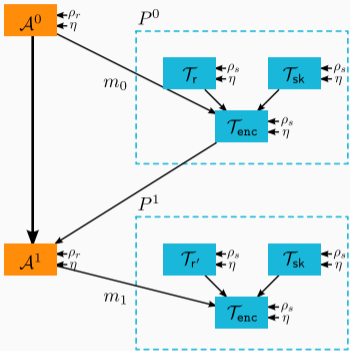


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Impossible with a quantum attacker

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Behind the curtain, the interpretation of terms crucially rely on two facts:

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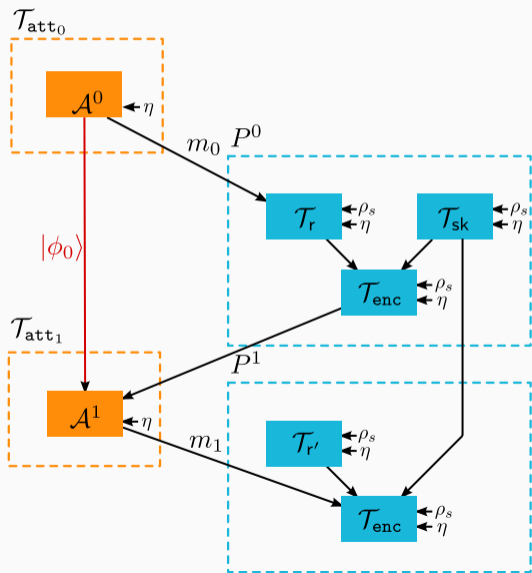
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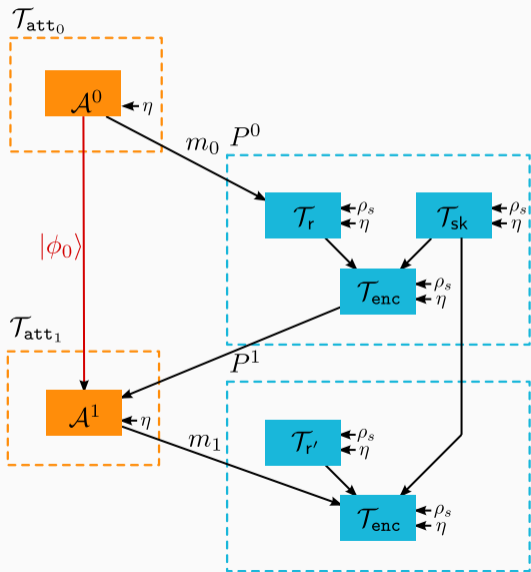
Our main contribution

An interpretation sound for **interactive black-box attackers**, where the interpretation directly depends a single interactive Turing Machine $\mathcal{T}_{\mathcal{A}}$, instead of many $\mathcal{T}_{\text{att}_i}$.

New (natural) interpretation

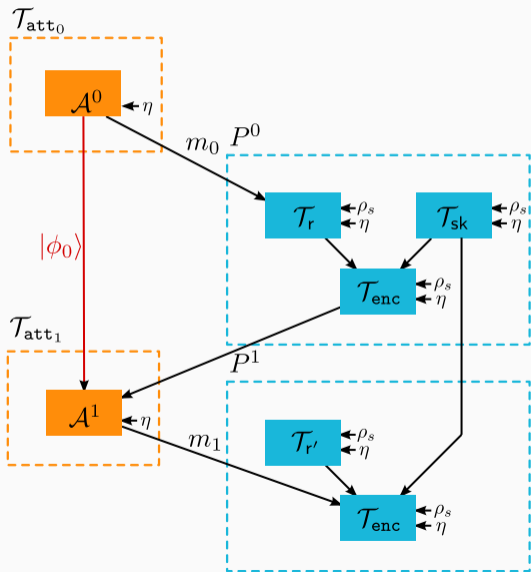


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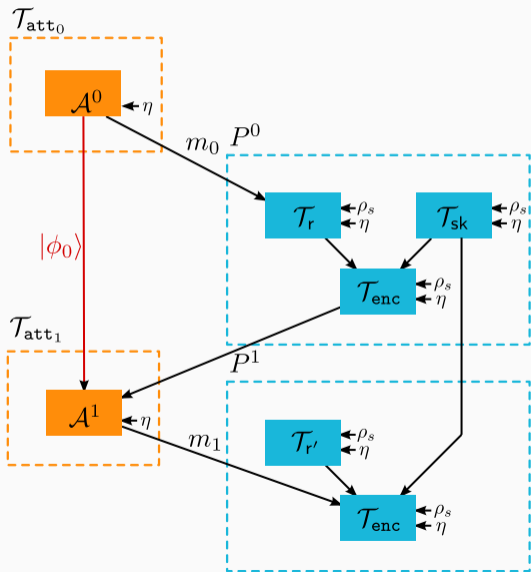
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↪ the single interactive attacker will know how many time it was called on both sides!

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- **Sufficient** to obtain the soundness of the BC logic;
- **Simple and syntactic**, so we were able to integrate them inside Squirrel with a few hundred lines of code, only at the cost of a small expressivity loss.

What is Squirrel

In a nut: an interactive prover for the BC logic

- Relies on a meta-logic to allow for **mechanized proofs of protocol** for an unbounded number of sessions;
- gives **computational guarantees**;
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Some figures

- 5 people core team: David Baelde, Stéphanie Delaune, Charlie J., Adrien Koutsos, Solène Moreau (and expanding)
- 30 000 lines of code and celebrating our 2 000 commit!
- about 15 real life case studies of protocols

Implementation and Case-studies

Protocol	LoC	Assumptions	Security properties
Key exchange protocols			
IkeV1 _{psk}	680	PRF, EUF-CMA	Strong Secrecy & Authentication
IkeV2 _{psk} ^{sign}	300	PRF, EUF-CMA	Strong Secrecy & Authentication
KE _{BCGNP}	355	PRF, IND-CCA, XOR	Strong Secrecy & Implicit Authentication
KE _{F_SXY}	660	PRF, IND-CCA, XOR	Strong Secrecy & Implicit Authentication
SC-AKE	650	PRF, IND-CCA, SUF-CMA, XOR	Strong Secrecy & Authentication
Proving post-quantum soundness of SQUIRRELcase studies			
Basic Hash	100	PRF, EUF-CMA	Authentication & Unlinkability
Hash Lock	130	PRF, EUF-CMA	Authentication & Unlinkability
LAK (with pairs)	250	PRF, EUF-CMA	Authentication & Unlinkability
MW	300	PRF, EUF-CMA, XOR	Authentication & Unlinkability
Feldhofer	270	ENC-KP, INT-CTXT	Authentication & Unlinkability
Private Authentication	100	IND-CCA, ENC-KP	Anonymity

What's next?

Recap

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The first **interactive protocol prover** that also provides **post-quantum guarantees**.

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Natural next step

Foundations for proving Key-Exchanges in Squirrel:

- Define how to express complex properties such as PFS or PCS in Squirrel, and simplified with our composition result.
- Link proofs in Squirrel with existing framework (BR, CK, eCK, ...)
- Perform an extensive case-study (KEMTLS)

The landscape

What we now have (thanks to 40 years of research!)

Many tools, attacker models and associated proof techniques. For instance:

- Proverif and Tamarin to verify at a high-level full protocol specifications;
- Squirrel to verify precisely the core of a protocol.

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Our goal

Build bridges inside the different groups in the community, as well as outside the community.

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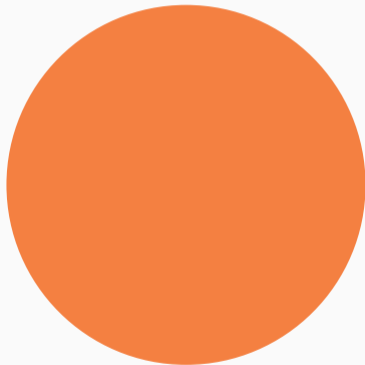
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- Then integrate Squirrel;
- Make a concrete multi-level analysis.



Formal Methods

One tool to use them all, and
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Cryptographers

Standardizations

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Long term goal

- attacker models for code level analysis, e.g. for fault-injection



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